

**2270-2, LINEAR ALGEBRA 01/18/05**  
**TRUE OR FALSE PROBLEMS IN CHAPTER 1**

Determine whether the following statement is True or False.

1. A system of four linear equations in three unknowns is always inconsistent.
2. There exists a  $3 \times 4$  matrix with rank 4.
3. If  $A$  is a  $3 \times 4$  matrix and vector  $\vec{v}$  is in  $\mathbb{R}^4$ , then vector  $A\vec{v}$  is in  $\mathbb{R}^3$ .
4. If the  $4 \times 4$  matrix  $A$  has rank 4, then any linear system with coefficient matrix  $A$

will have a unique solution.

5.  $\text{rank} \begin{bmatrix} 2 & 2 & 2 \\ 2 & 2 & 2 \\ 2 & 2 & 2 \end{bmatrix} = 2.$

6. There exists a matrix  $A$  such that  $A \begin{bmatrix} -1 \\ 2 \end{bmatrix} = \begin{bmatrix} 3 \\ 6 \\ 7 \end{bmatrix}.$

7. Vector  $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  is a linear combination of  $\begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$  and  $\begin{bmatrix} 7 \\ 8 \\ 9 \end{bmatrix}.$

8. If  $A$  is a nonzero matrix of the form  $\begin{bmatrix} a & -b \\ b & a \end{bmatrix}$  then the rank of  $A$  must be 2.

9. If  $A$  and  $B$  are matrices of the same size, then the formula  $rk(A+B) = rk(A) + rk(B)$  must hold.

10. If  $A$  is a  $3 \times 4$  matrix of rank 3, then the system  $A\vec{x} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  must have infinitely many solutions.