

H3.3-16 Derive Fourier coefficient formulas
for Fourier series on $a \leq x \leq b$.

Hint: $y = \frac{a+b}{2} + \frac{b-a}{2} \frac{x}{L}$



Solve for x in terms of y

$$2y = a+b + (b-a) \frac{x}{L}$$

$$\frac{2y}{b-a} = \frac{a+b}{b-a} + \frac{x}{L}$$

$$x = L \left(\frac{2y}{b-a} - \frac{a+b}{b-a} \right)$$
$$\frac{n\pi x}{L} = \frac{2n\pi y}{b-a} - \frac{(a+b)n\pi}{b-a}$$