

```
> # Compute and plot full sine and cosine series, sine series,
  cosine series
```

```
> L:=1;f:=x->1+x;
```

$L:=1$

(1)

```
> # Truncated sine series S(x,n)
```

```
> B:=n->(2/L)*int(f(x)*sin(n*Pi*x/L),x=0..L);
```

$$B := n \rightarrow \frac{2 \left(\int_0^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx \right)}{L}$$

(2)

$f := x \rightarrow 1 + x$

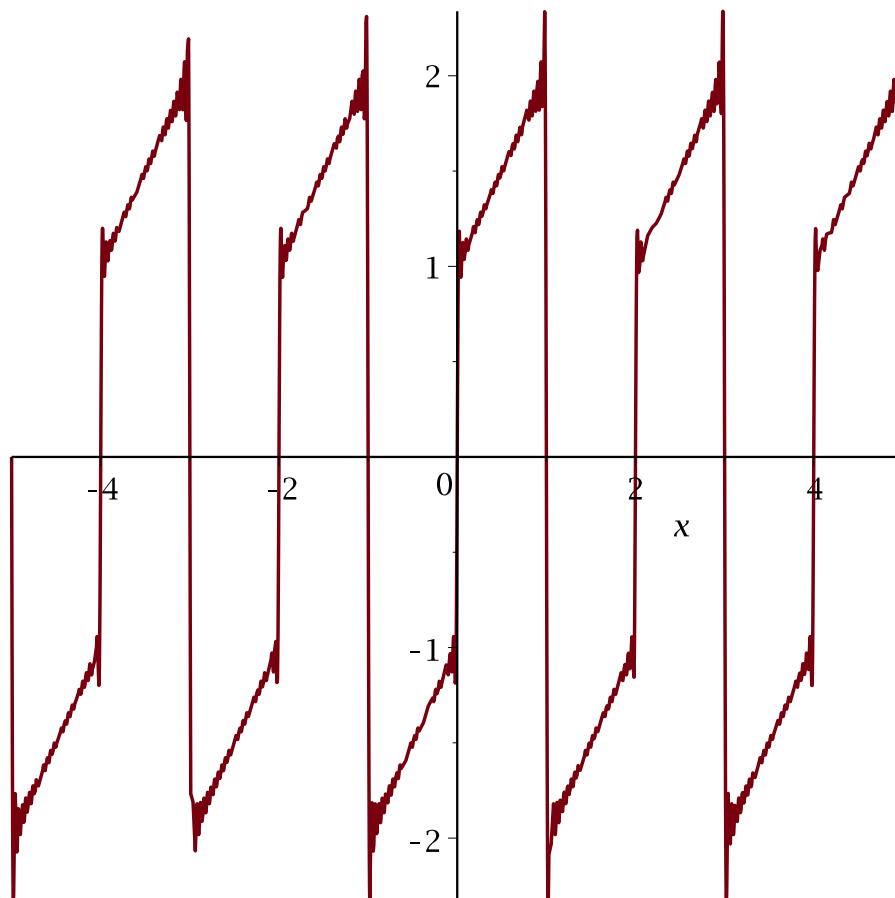
(3)

```
> S:=(x,n)->sum(B(k)*sin(k*Pi*x/L),k=1..n);
```

$$S := (x, n) \rightarrow \sum_{k=1}^n B(k) \sin\left(\frac{k\pi x}{L}\right)$$

(4)

```
> plot(S(x,50),x=-5*L..5*L);
```



```
> A:=n->(2/L)*int(f(x)*cos(n*Pi*x/L),x=0..L);
```

$$A := n \rightarrow \frac{2 \left(\int_0^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx \right)}{L} \quad (5)$$

```
> A0:=(1/L)*int(f(x),x=0..L);
```

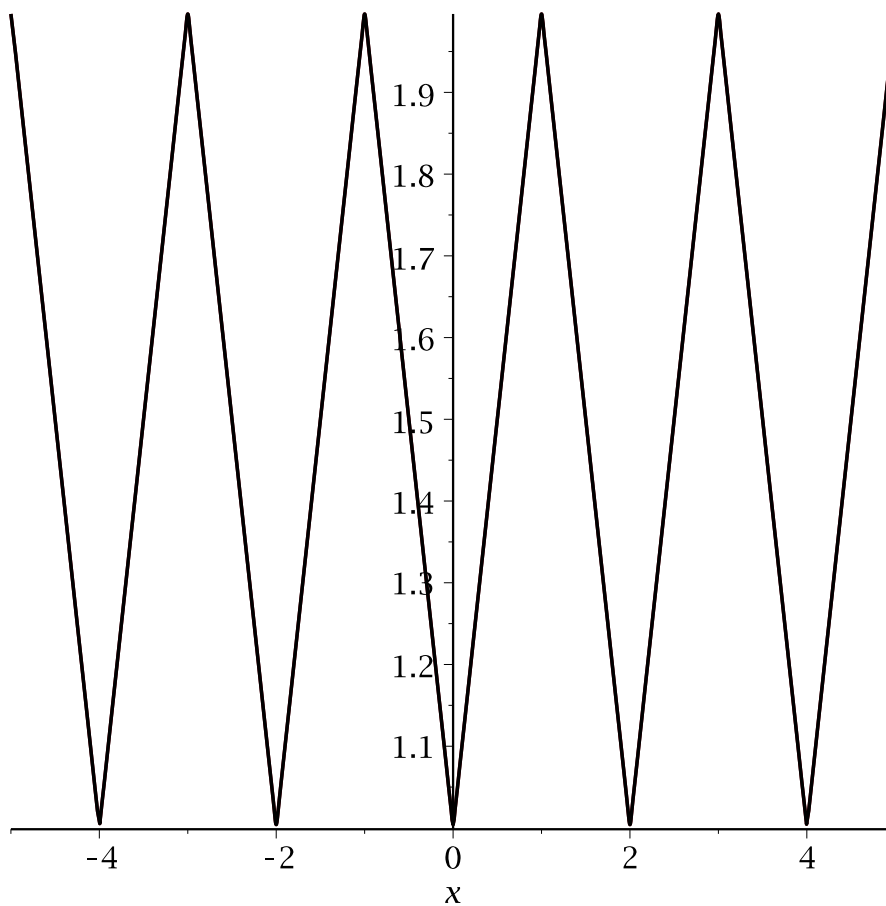
$$A0 := \frac{3}{2} \quad (6)$$

```
> # Truncated cosine series T(x,n)
```

```
> T:=(x,n)->A0+sum(A(k)*cos(k*Pi*x/L),k=1..n);
```

$$T := (x, n) \rightarrow A0 + \sum_{k=1}^n A(k) \cos\left(\frac{k\pi x}{L}\right) \quad (7)$$

```
> plot(T(x,50),x=-5*L..5*L);
```



```
> # # Truncated full Fourier sine and cosine series R(x,n)
```

```
> a:=n->(2/2*L)*int(f(x)*cos(n*Pi*x/L),x=-L..L);a0:=(1/(2*L))*int(f(x),x=-L..L);
```

$$a := n \rightarrow L \left(\int_{-L}^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx \right)$$

$$a0 := 1 \quad (8)$$

> `b:=n->(2/(2*L))*int(f(x)*sin(n*Pi*x/L),x=-L..L);`

$$b := n \rightarrow \frac{\int_{-L}^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx}{L} \quad (9)$$

> `R:=(x,n)->a0+sum(a(k)*cos(k*Pi*x/L),k=1..n)+sum(b(k)*sin(k*Pi*x/L),k=1..n);`

$$R := (x, n) \rightarrow a0 + \sum_{k=1}^n a(k) \cos\left(\frac{k\pi x}{L}\right) + \sum_{k=1}^n b(k) \sin\left(\frac{k\pi x}{L}\right) \quad (10)$$

> `plot(R(x,50),x=-5*L..5*L);`

