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> # Find Fourier sin coefficients for
# f(x)=1 on x<L/6, f(x)=3 on L/6<x<L/2, f(x)=0 elsewhere
> L:=1;

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$$L := 1 \quad (1)$$

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> f:=x->piecewise(x<0,0, x<L/6,1,x<L/2, 3, 0);

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$$f := x \rightarrow \text{piecewise}\left(x < 0, 0, x < \frac{1}{6} L, 1, x < \frac{1}{2} L, 3, 0\right) \quad (2)$$

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> convert(f(x),piecewise,x);

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$$\left\{ \begin{array}{ll} 0 & x < 0 \\ 1 & x < \frac{1}{6} \\ 3 & x < \frac{1}{2} \\ 0 & \frac{1}{2} \leq x \end{array} \right. \quad (3)$$

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> # Truncated sine series S(x,n)

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> B:=n->eval((2/L)*int(f(x)*sin(n*Pi*x/L),x=0..L));

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$$B := n \rightarrow \text{eval}\left(\frac{2 \left(\int_0^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx \right)}{L}\right) \quad (4)$$

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> B(1);

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$$-\frac{-2 + \sqrt{3}}{\pi} + \frac{3\sqrt{3}}{\pi} \quad (5)$$

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> B(n) assuming n > 0;

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$$-\frac{2 \left(-1 + \cos\left(\frac{1}{6} n\pi\right) \right)}{n\pi} + \frac{6 \left(\cos\left(\frac{1}{6} n\pi\right) - \cos\left(\frac{1}{2} n\pi\right) \right)}{n\pi} \quad (6)$$