

Superposition

Can't use \sum

add $T(t) \mathcal{E}(x) = e^{-\frac{w^2}{4}kt} (A(w) \cos(wx) + B(w) \sin(wx))$

$0 \leq w < \infty$

$$u(x,t) = \sum \text{prod sols} = \sum_n e^{-\frac{w_n^2}{4}kt} (A(w_n) \cos(w_n x) + B(w_n) \sin(w_n x)) \Delta w_n \underset{\substack{w=0 \\ w=\infty}}{\simeq} \int e^{-\frac{w^2}{4}kt} (A(w) \cos(wx) + B(w) \sin(wx)) dw$$

$$f(x) = u(x,0) = \int_0^\infty (A(w) \cos(wx) + B(w) \sin(wx)) dw$$

