## Mathematics 1210 Prof. Ken Golden PRACTICE FINAL EXAM Fall 2018

Problems From Varberg, et al. (Chapter.Section.Number)

- 1. 5.1.6. Use the three step procedure (slice, approximate, integrate) to set up an integral for the area of the region lying above the parabola  $y = x^2 2$ , below the line y = x + 4, and enclosed by these two graphs.
- 2. 5.2.17. Find the volume of the solid generated by revolving about the x-axis the region bounded by the upper half of the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

and the x-axis, and thus find the volume of a prolate spheroid. Here a and b are positive constants, with a > b.

- 3. 5.3.2. Find the volume of the solid generated when the region R bounded by the curves  $y=x^2, x=1, y=0$  is revolved about the y-axis. Do this by performing the following steps: (a) Sketch the region R. (b) Show a typical rectangular slice properly labeled. (c) Write a formula for the approximate volume of the shell generated by this slice. (d) Set up the corresponding integral. (e) Evaluate this integral.
- 4. 5.4.10. Sketch the graph of the parametric equation

$$x(t) = \sqrt{5}\sin 2t - 2,$$
  $y(t) = \sqrt{5}\cos 2t - \sqrt{3},$   $0 \le t \le \frac{\pi}{4},$ 

and find its length.

5. 5.4.21a. Find the length of the curve

$$y = \int_{1}^{x} \sqrt{u^3 - 1} \ du, \quad 1 \le x \le 2.$$

- 6. 5.5.6. For a certain type of nonlinear spring, the force required to keep it stretched a distance s is given by the formula  $F = ks^{4/3}$ . If the force required to keep it stretched 8 inches is 2 pounds, how much work is done in stretching this spring 27 inches?
- 7. 5.5.22. According to Coulomb's Law, two like electrical charges repel each other with a force that is inversely proportional to the square of the distance between them. If the force of repulsion is 10 dynes (1 dyne =  $10^{-5}$  newton) when they are 2 centimeters apart, find the work done in bringing the charges from 5 centimeters apart to 1 centimeter apart.
- 8. 5.6.25. Use Pappus's Theorem to find the volume of the solid obtained when the region bounded by  $y = x^3$ , y = 0, and x = 1 is revolved about the y-axis. Do the same problem by the method of cylindrical shells to check your answer.

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9. Find the temperature profile T(x) on the interval [0,1] satisfying the steady state heat equation

$$\frac{d^2T}{dx^2} = 0$$

and the boundary conditions T(0) = 4 and T(1) = 2.

10. A ball is thrown upward from the ground on Earth with initial velocity 32 f/s, so that its velocity as a function of time is given by v(t) = -32t + 32. Use this velocity function to find the net displacement and total distance travel on the time interval [0,2] seconds.