Midterm 1 Review Guide

1 Chapter 0

You should be familiar with all of the review material, especially anything that was covered in class or on the first homework assignment.

2 Chapter 1

2.1 Section 1

- 1. Situations where there is not a limit (jumps, endpoints, wiggles too much)
- 2. Left and Right limits
- 3. Theorem 1.1A (there is only a limit if the left limit equals the right limit)

2.2 Section 3

- 1. Main Limit Theorem (be able to use the 9 rules to simplify limits, you do not need to have all 9 rules memorized by number)
- 2. Know how to evaluate the limits of polynomial and rational functions, especially what to do if the rational function is dividing by zero at the limit point.
- 3. Squeeze Theorem. Know how to use a picture where u(x) and l(x) are given to prove that f(x) has a limit.

2.3 Section 4

- 1. Know the limits of simple trig functions (Theorem 1.4A)
- 2. Know the 2 special trig limits $(\sin x)/x$ and $(1-\cos x)/x$ (Theorem 1.4B)
- 3. Be able to use these rules to solve the limits of more complicated functions made of trig functions

2.4 Section 5

- 1. Know how to take the limit of functions and sequences at plus or minus infinity
- 2. Know how to take limits of functions with horizontal and vertical asymptotes

2.5 Section 6

- 1. Know what it means for a function to be continuous at a point (Theorem 1.6A)
- 2. Know how to fix the discontinuity of a removably discontinuous function (for example HW problem 1.6.20)

3 Chapter 2

3.1 Section 1

1. Understand the different types of problems that all mean the same thing (Derivative = slope of tangent line = instantaneous velocity/rate of change)

3.2 Section 2

- 1. Know the different limit definitions of the derivative and how to use them to evaluate a derivative
- 2. Differentiable implies continuous, know why the opposite is not true
- 3. Know examples of how functions are not differentiable at a point (corners, holes, endpoints, vertical tangents, wiggles too much, etc.)
- 4. Be able to sketch a graph of f' if you are given the graph of f.

3.3 Section 3

1. Know the derivative rules (power, product, quotient, etc.) and be able to use them together to find the derivatives of more complicated functions.

3.4 Section 4

1. Know the simple trig function derivatives

3.5 Section 5

1. Know the definition of the chain rule and how to use it to find the derivative of more complicated functions

3.6 Section 6

- 1. Know the different notations for higher order derivatives and how to take them.
- 2. Know what happens to sin, cos, and polynomial functions as you take higher order derivatives.

3.7 Section 7

1. Know how to take the derivatives of equations/relations which are not necessarily functions with implicit differentiation using the chain rule on y(x)

3.8 Section 8

- 1. Know how to set up related rates equations
- 2. Know how to use implicit differentiation to solve for derivatives of related rates equations

4 Homework Problems

Understand and be able to do all of the homework assignments (1-4)

5 Practice Midterm

Understand and be able to solve all of the problems from the practice midterm.