## Vectors \& Scalars

## Vectors

$\mathbb{R}^{2}$ is the set of all pairs of real numbers. In the context of drawing graphs, the objects in $\mathbb{R}^{2}$ are called points, and pairs are written left-to-right, so that $(3,2)$ is the point in $\mathbb{R}^{2}$ whose $x$-coordinate equals 3 and whose $y$-coordinate equals 2 .

In the context of linear algebra, the objects in $\mathbb{R}^{2}$ are called vectors, and instead of being written left-to-right, they are usually written top-to-bottom. Written in this way, the vector in $\mathbb{R}^{2}$ whose $x$-coordinate is 3 and whose $y$-coordinate is 2 is

$$
\binom{3}{2}
$$

$\mathbb{R}^{3}$ is the set of all "triples" of real numbers. An object in $\mathbb{R}^{3}$ - also called a vector - has an $x$-coordinate, a $y$-coordinate, and a $z$-coordinate. When writing vectors in $\mathbb{R}^{3}$, the $x$-coordinate is on top, the $y$-coordinate is directly below, and the $z$-coordinate is on the bottom. Thus

$$
\left(\begin{array}{r}
5 \\
0 \\
-1
\end{array}\right)
$$

is the vector in $\mathbb{R}^{3}$ where $x=5, y=0$, and $z=-1$.

## Vector addition

To add two vectors in $\mathbb{R}^{2}$ - or two vectors in $\mathbb{R}^{3}$ - add each of their coordinates.

## Examples.

$$
\binom{-5}{1}+\binom{4}{2}=\binom{-5+4}{1+2}=\binom{-1}{3}
$$

and

## Scalar multiplication

In linear algebra, real numbers are often called scalars. You cannot multiply two vectors, but you can multiply a scalar and a vector. To do so, multiply every coordinate in the vector by the scalar.

## Examples.

$$
2\binom{7}{-3}=\binom{2(7)}{2(-3)}=\binom{14}{-6}
$$

and

$$
\begin{aligned}
& 5\left(\begin{array}{r}
-1 \\
0 \\
4
\end{array}\right)=\left(\begin{array}{c}
5(-1) \\
5(0) \\
5(4)
\end{array}\right)=\left(\begin{array}{c}
-5 \\
0 \\
20
\end{array}\right) \\
& * * * * * * * * * *
\end{aligned}
$$

## Exercises

1.) Find

$$
\binom{-5}{1}+\binom{4}{2}
$$

2.) Find

$$
\left(\begin{array}{l}
4 \\
2 \\
6
\end{array}\right)+\left(\begin{array}{r}
3 \\
-8 \\
0
\end{array}\right)
$$

3.) Find

$$
2\binom{7}{-3}
$$

4.) Find

$$
5\left(\begin{array}{r}
-1 \\
0 \\
4
\end{array}\right)
$$

