The study of sample path intersections is partially motivated by the needs in mathematical physics. In this talk I will try to describe the large deviations for the self-intersection local times, mutual intersection local times, ranges and the intersection of ranges generated by random walks of lattice-values. In particular, I will talk about some unsolved problems and conjectures on these models.