## **Stochastics Seminar** Department of Mathematics, University of Utah



## Independent Constants and Some Gaussian Inequalities

## Wenbo V. Li

University of Delaware **Time and Place:** Wednesday April 19, 2006; 3:30–4:25 p.m.; JWB 308

Given *d* real-valued random variables  $X_1, \dots, X_d$ , there are various ways to measure dependence-structures among them. They include measuring correlations, mixed moments, etc. In this talk, we define and study a new measure that captures the amount of dependence when it is compared with the "best" independent ones. To be more precise, we consider the best (largest constant  $\alpha$  and smallest constant  $\beta$ ) possible probability bounds

$$\alpha \prod_{i=1}^{d} \mathbb{P}(W_i \in B_i) \leq \mathbb{P}\left(\bigcap_{i=1}^{d} \{X_i \in B_i\}\right) \leq \beta \prod_{i=1}^{d} \mathbb{P}(Y_i \in B_i),$$

for some real valued random variables  $W_i$ ,  $Y_i$ , and all Borel sets  $B_i$ ,  $1 \le i \le d$ . The joint Gaussian case will be discussed in detail.