

Name:

1. Using the method of undetermined coefficients, solve the differential equation

$$y'' + 4y = x \sin(x) + 8$$

2. Using variation of parameters, solve the differential equation

$$y'' - 4y = \sinh(2x)$$

3. Use Laplace transforms to solve the initial value problem

$$\begin{aligned}x'' + 4x &= \sin(3t), \\x(0) &= x'(0) = 0\end{aligned}$$

4. Find the transient motion and steady periodic oscillations of a damped mass and spring system with $m=1$, $c=2$, and $k=26$ under the influence of an external force $F(t)=82\cos(4t)$, with $x(0)=6$ and $x'(0)=0$.

5. Apply the convolution theorem to find the inverse Laplace transform of the function

$$F(s) = \frac{1}{s(s^2+4)}.$$

A short table of Laplace Transforms	
$f(t)$	$F(s)$
1	$\frac{1}{s} \ (s > 0)$
t	$\frac{1}{s^2} \ (s > 0)$
$t^n \ (n \geq 0)$	$\frac{n!}{s^{n+1}} \ (s > 0)$
e^{at}	$\frac{1}{s-a} \ (s > 0)$
$\cos(kt)$	$\frac{s}{s^2+k^2} \ (s > 0)$
$\sin(kt)$	$\frac{k}{s^2+k^2} \ (s > 0)$
$\cosh(kt)$	$\frac{s}{s^2-k^2} \ (s > k)$
$\sinh(kt)$	$\frac{k}{s^2-k^2} \ (s > k)$
$u(t-a)$	$\frac{e^{-as}}{s} \ (s > 0)$