

MATH 5075 R Project 1

Your Name Here

October 3, 2016

Remember: I expect to see commentary either in the text, in the code with comments created using #, or (preferably) both! **Failing to do so may result in lost points!**

Because randomization is used in this assignment, I set the seed here, in addition to beginning each code block. **Do not change the seed!**

```
set.seed(6222016)
```

Problem 1

1. Simulate 150 observations from the following process using the functions `rnorm()` and `filter()`:

$$x_t = 0.5x_{t-1} - 0.4x_{t-2} + w_t$$

($w_t \sim N(0, 1)$) Discard the first 50 observations; this represents the “burn-in” period.

```
# Your code here
```

2. Figure out how to use the function `lm()` to find the OLS estimate for the parameters in the models:

$$x_t = \mu + \phi_1 x_{t-1} + w_t$$

$$x_t = \mu + \phi_1 x_{t-1} + \phi_2 x_{t-2} + w_t$$

$$x_t = \mu + \phi_1 x_{t-1} + \phi_2 x_{t-2} + \phi_3 x_{t-3} + w_t$$

using the data obtained in part 1. Report the estimated parameters and their significance levels, the R^2 value, and the F statistic with the associated p -value assessing the fit of the model. Which model appears to provide the best fit? Plot the residuals for each model. Do the residuals appear to be a white noise process? (Hint: consider making a data frame where the lags are the variables upon which you regress.)

```
# Your code here
```

Problem 2

The data set `gtemp` (`astsa`) contains data on global temperatures. This is an R `ts` object.

1. What span of time is covered by the data in `gtemp`? What is the data’s frequency (is it semiannual, annual, biannual, monthly, etc.)?

```
# Your code here
```

2. Plot the data in `gtemp`. Is this a stationary process?

```
# Your code here
```

3. Use `diff()` to find the first difference of the data; this represents change in temperature. Plot the result. Does this appear to be a stationary process?

```
# Your code here
```

4. Use the function `lm()` to fit the following model on the first differences of `gtemp`:

$$y_t = \mu + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \phi_3 y_{t-3} + w_t$$

```
# Your code here
```