Projects Dynamics of species

m 5740, Spring 2014

Please read all five projects. Choose your preferences.

Each project should be done by one or two groups. The group prepares the powerpoint or pdf presentation and writes a complementary note if needed. After the class presentation and questions-answers session, the presentation can be corrected before final submission.

The presentations start next week. Plan for 17 minute talk and 6 minutes of questions. Bring you computer or send me the file. Practice presenting the material; at home, your talk should last 13-14 minutes (a speaker needs an additional time because of the stress of a public speech).

A Leslie model and a modificaion

- Introduce Leslie model, find data
- Find stable age distribution and the growth rate. Compute the dynamics. Graph the results
- Modify the model by adding a stabilizer: assume that the growth rate depends on the size of the population. Compute the dynamics
- **B** Reaction-diffusion equation: Allee model with a diffusion term
 - Describe the model, simulate the dynamics. What happens when diffusivity is zero (is infinity)
 - Assume that initial data P(n, 0) are below and above the threshold value K is different points, for example P(1, 0) = .5K, P(2, 0) = 1.5K, etc. Experiment with various initial data sets.

Impose periodic boundary conditions: P(0,m) = P(n,m), P(1,m) = P(n+1,m) for all m.

C Species interaction and competition.

Consider a model with two species X and Y that compete for a resource and a predator Z that preys on them.

$$\dot{X} = \alpha_1 X - \beta_1 X Y - \gamma_1 X Z$$
$$\dot{Y} = \alpha_2 Y - \beta_2 X Y - \gamma_2 Y Z$$
$$\dot{Z} = -\alpha_3 Y + \delta_3 X Z - \delta_3 Y Z$$

- Find the equilibrium points. Investigate their stability
- Simulate the dynamics, using different initial conditions, $X(0) \ll Y(0)$, and $X(0) \gg Y(0)$. (You may consider either differential on difference model.)
- **D** Delay equation in population dynamics
 - Read "DELAY DIFFERENTIAL EQUATIONS IN SINGLE SPECIES DYNAMICS" by Shigui Ruan (http://www.math.miami.edu/ ruan/MyPapers/Ruan-nato.pdf)
 - Present the technique of delay equations, and illustrate them using logistic growth and Allee model with delay.
 - Discuss instabilities and bifurcations.
- E Epidemics spread
 - Read Wikipedia articles

 en.wikipedia.org/wiki/Epidemic_model,
 en.wikipedia.org/wiki/Compartmental_models_in_epidemiology,
 and (as a complement)
 en.wikipedia.org/wiki/Mathematical_modelling_of_infectious_disease
 - Describe and simulate SIR, SIRS, SEIS models. Explain the difference

You may use either differential or difference equations.