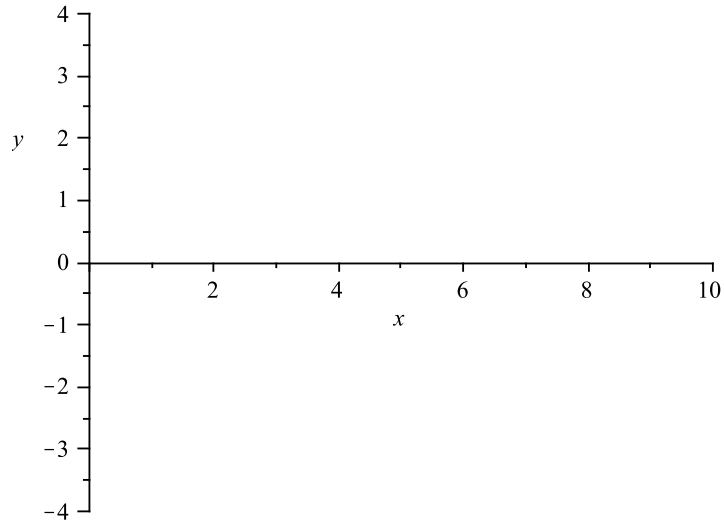
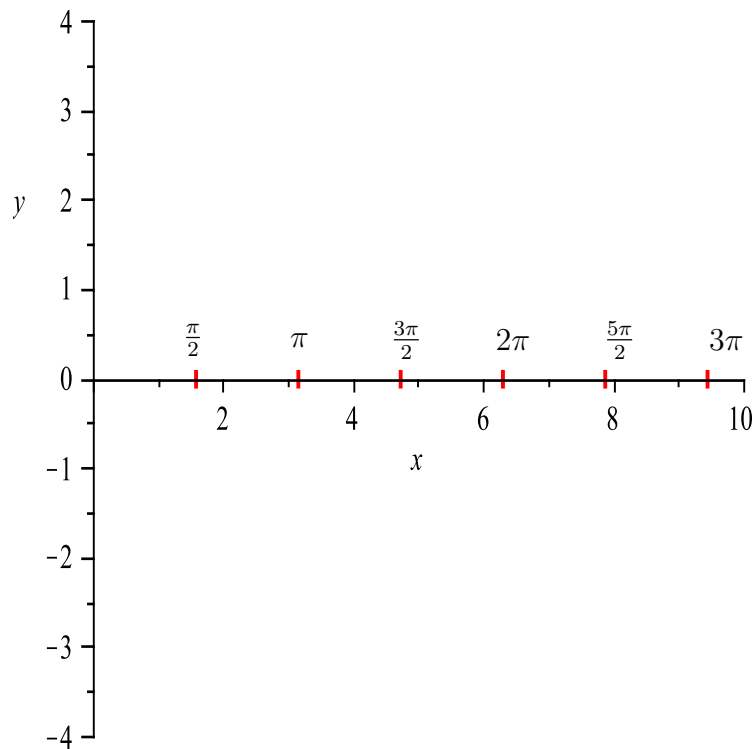


## Solutions

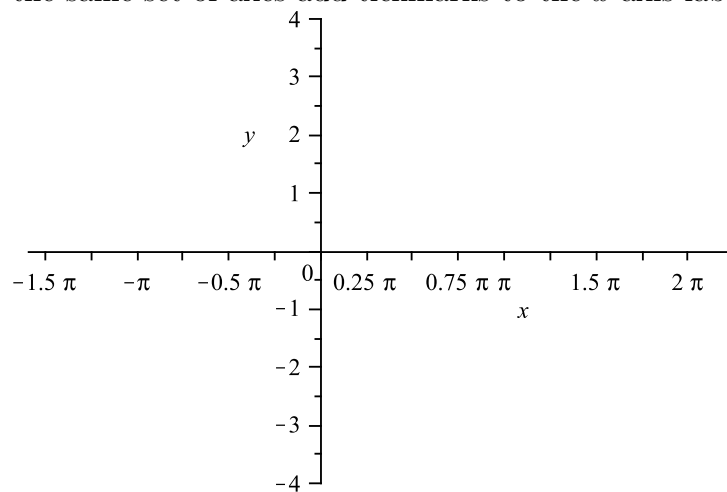
1. Below is a set of axes. The tickmarks on the  $x$ -axis are labeled with integers. On the same set of axes add tickmarks to the  $x$ -axis labeled with multiples of  $\frac{\pi}{2}$ .



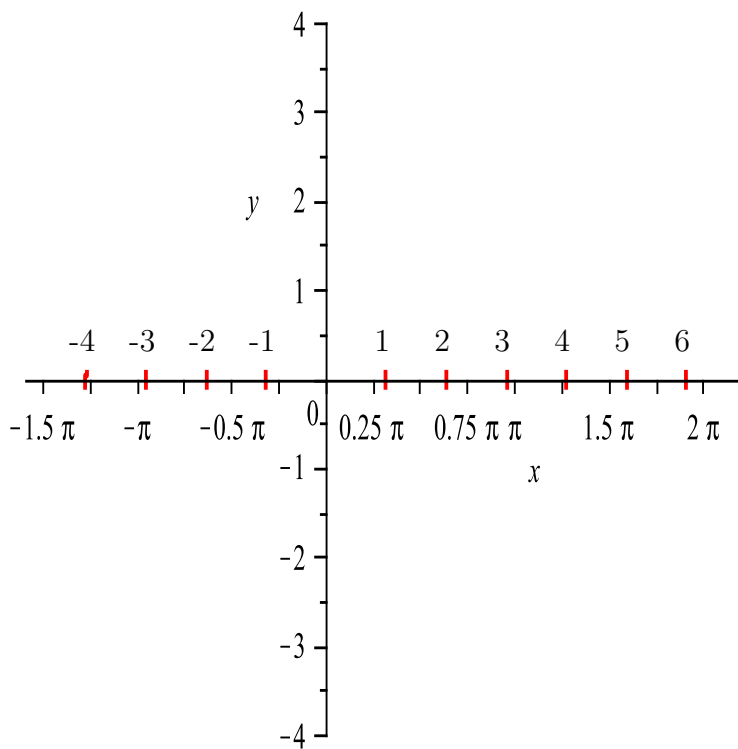
**Solution:**



2. Below is a set of axes. The tickmarks on the  $x$ -axis are labeled with multiples of  $\frac{\pi}{4}$ . On the same set of axes add tickmarks to the  $x$ -axis labeled with integers.



**Solution:**



3. For  $2 \sin(3x - \pi) + 1$  give the

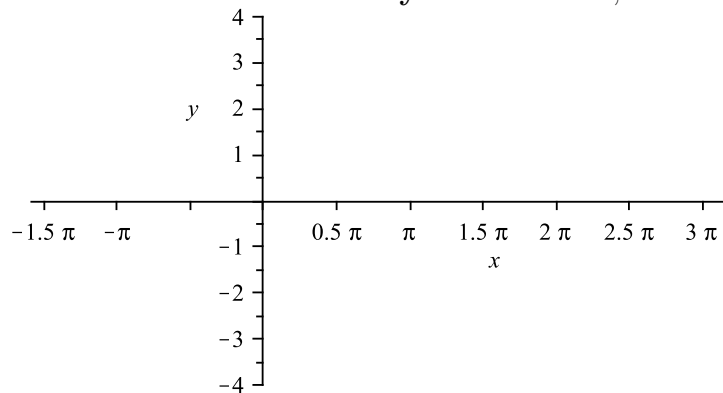
- amplitude
- period
- phase shift

- vertical shift

**Solution:**

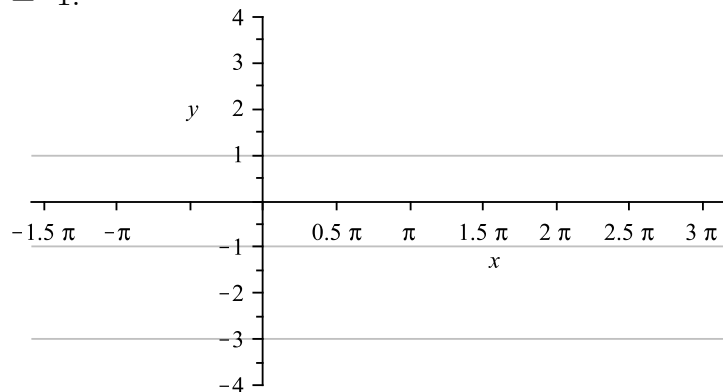
- amplitude=2
- period= $\frac{2\pi}{3}$
- phase shift= $\frac{\pi}{3}$
- vertical shift=1

4. Consider a sine curve with amplitude=2, period= $\pi$ , phase shift=1, and vertical shift=-1. On the axes below draw **only** the minimum, maximum and equilibrium lines.

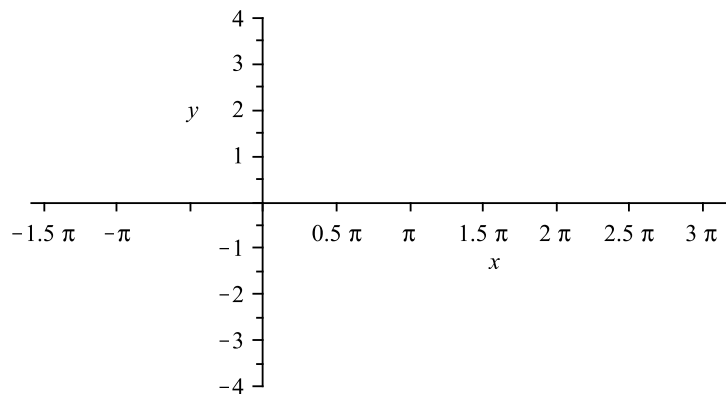


**Solution:**

Maximum line is at height=vertical shift + amplitude =  $-1 + 2 = 1$ . Minimum line is at height=vertical shift - amplitude =  $-1 - 2 = -3$ . Equilibrium line is at height=vertical shift = -1.

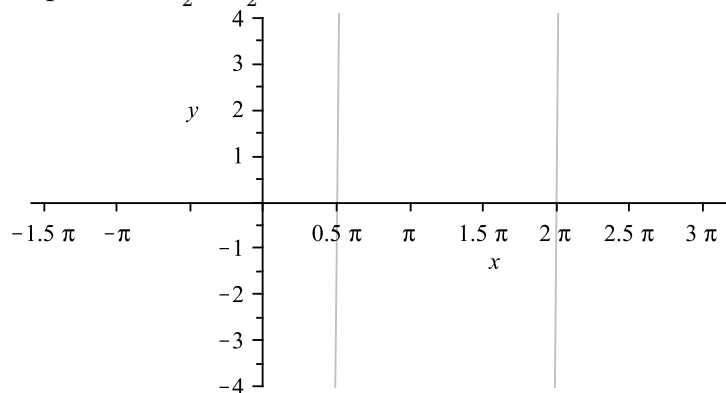


5. Consider a sine curve with amplitude=1, period= $\frac{3\pi}{2}$ , phase shift= $\frac{\pi}{2}$ , and vertical shift=-1. On the axes below draw **only** a vertical starting line and ending line.



**Solution:**

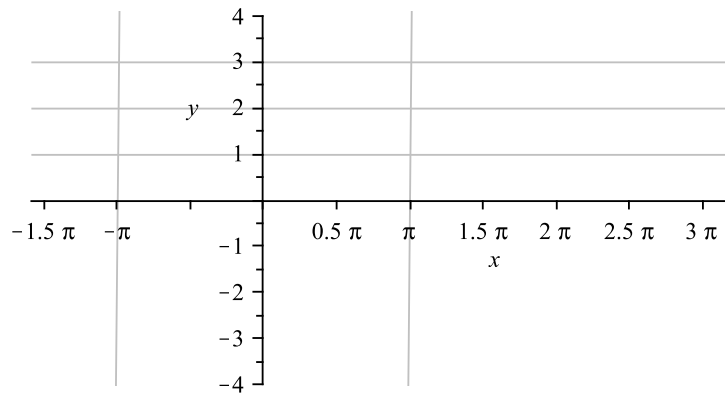
Starting line has  $x$ -coordinate = phase shift =  $\frac{\pi}{2}$ . Ending line has  $x$ -coordinate = phase shift + period =  $\frac{\pi}{2} + \frac{3\pi}{2} = 2\pi$ .



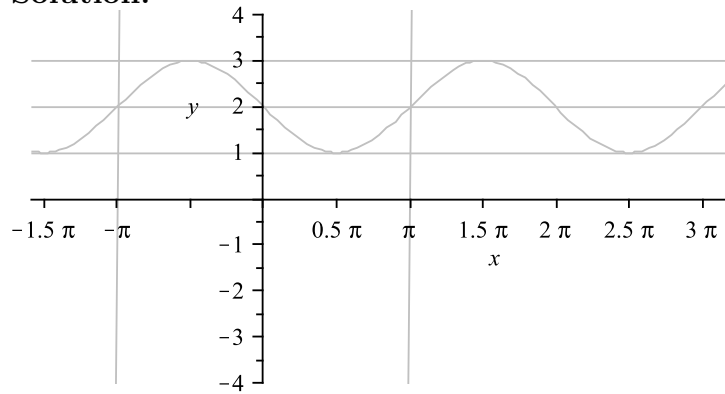
6. On the axes below you are given the maximum, minimum, equilibrium, starting and ending lines. Draw in a sine curve (the entire curve, not just one cycle). What are the

- amplitude
- period
- phase shift
- vertical shift

for the curve?



**Solution:**



- amplitude = 1 = distance between maximum and equilibrium lines.
- period =  $2\pi$  = distance between starting and ending lines.
- phase shift =  $-\pi$  =  $x$ -coordinate of starting line.
- vertical shift = 2 =  $y$ -coordinate of equilibrium line.