

- 1) b) critical points: $x=2, 5, 9, 11$, any point between 11 and 14
 points of inflection: $x=3, 8$,
 c) discontinuous at $x=11$
 d) increasing: $x<2, 5<x<9$
 decreasing $2<x<5, 9<x<11, x>14$
 constant $11<x<14$
 concave up $3<x<8$
 concave down $x<3, 8<x<11, x>14$
- 2) a) $30 \exp(3x)$
 b) $(10s(3s-2)-3(5s^2-1))/(3s-2)^2 = (15s^2-20s+3)/(3s-2)^2$
- 3) $f'(w)=1/w$
 $f''(w)=-1/w^2$
4. a) Steady states: $x^*=(x^*)^2$
 $x^*=0$ and $x^*=1$
 stability: updating function $f(x)=x^2$
 $f'(x)=2x$
 $f'(0)=0$; $-1<f'(0)<1$, i.e. $x^*=0$ is stable
 $f'(1)=2$; $f'(1)>1$, i.e. $x^*=1$ is unstable
 b) The solution will get further away from 1 and closer to 0, without oscillations, so if we wait for a long time we will get close to $x(t)=0$
- 5) a) $M(V)=1.3V$
 $V(L)=2L^3$
 $L(T)=10+T/10$
 $M(T)=M(V(L(T)))$
 $M'(T)=M'(V)*V'(L)*L'(T)=1.3*6L^2*0.1=0.78(10+T/10)^2$
- b) $M'(T)>0$, i.e. the insect will be gaining weight
- 6) a) $s^*=0$
 b) $f'(x)=-0.8$, so $s^*=0$ is stable
 d) each time step the solution alternates between positive and negative value, with diminishing amplitude
 e) it will oscillate around zero, getting closer and closer to zero.
- 7) $w_{t+1}=2w_t/(2w_t+3(1-w_t))=2w_t/(3-w_t)$ (missing condition: plants will descendants with the same color of flowers)