

Derivatives

$$D_x(e^x) = e^x$$

$$D_x(\ln x) = \frac{1}{x}$$

$$D_x(x^a) = ax^{a-1}$$

$$D_x(a^x) = (\ln a)a^x$$

$$D_x(\sin x) = \cos x$$

$$D_x(\cos x) = -\sin x$$

$$D_x(\tan x) = \sec^2 x$$

$$D_x(\cot x) = -\csc^2 x$$

$$D_x(\sec x) = \sec x \tan x$$

$$D_x(\csc x) = -\csc x \cot x$$

$$D_x(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}, x \in (-1,1)$$

$$D_x(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}}, x \in (-1,1)$$

$$D_x(\tan^{-1} x) = \frac{1}{1+x^2}$$

$$D_x(\sec^{-1} x) = \frac{1}{|x|\sqrt{x^2-1}}, |x| > 1$$

Miscellaneous

$$\lim_{h \rightarrow 0} (1+h)^{1/h} = e$$

To solve $\frac{dy}{dx} + P(x)y = Q(x)$, multiply both sides by $e^{\int P(x)dx}$ and solve.

More Derivatives

$$D_x(\sinh x) = \cosh x$$

$$D_x(\cosh x) = \sinh x$$

$$D_x(\operatorname{csc} hx) = -\operatorname{csc} hx \coth x$$

$$D_x(\tanh x) = \operatorname{sech}^2 x$$

$$D_x(\operatorname{sec} hx) = -\operatorname{sec} hx \tanh x$$

$$D_x(\operatorname{coth} x) = -\operatorname{csc} h^2 x$$

$$D_x(\sinh^{-1} x) = \frac{1}{\sqrt{x^2+1}}$$

$$D_x(\cosh^{-1} x) = \frac{1}{\sqrt{x^2-1}}, x > 1$$

$$D_x(\tanh^{-1} x) = \frac{1}{1-x^2}, -1 < x < 1$$

$$D_x(\operatorname{sec} h^{-1} x) = \frac{-1}{x\sqrt{1-x^2}}, 0 < x < 1$$