

**Math 5110: Homework Assignment 5**  
**Due Sep 26, 2017**

1. Consider the Nicholson-Bailey model in the case that each parasitoid produces  $c$  offspring rather than just one as in the standard equations. Find the equilibria and their stability. Can low parasitoid reproduction stabilize the equations?
2. Suppose that a population of hosts and parasitoids follow the Nicholson-Bailey equations but that each year a fraction  $p$  of the hosts have a safe refuge from attack.
  - a. Find the equilibria and their stability.
  - b. How is this different from a case where there are  $S$  safe sites, and only  $N_t - S$  hosts are available for attack?
  - c. Modify the R program to simulate this case.
3. Suppose that instead of having a safe place to hide, hosts have a safe age. In particular, adults are vulnerable to attack, with a proportion  $e^{-aP_t}$  surviving long enough to make  $\lambda$  offspring. However, offspring are not attacked by parasitoids, and a fraction of  $\sigma$  survive to adulthood. Development takes exactly two years for hosts and one year for the parasitoids. Can this invulnerable age class stabilize the interaction?