Instructions. Show all work and include appropriate explanations when space is provided. Correct answers unaccompanied by work may not receive full credit. Please circle your final answer. The last page contains some useful identities.

1. (30pts) Find the indicated derivatives. No need to simplify.
   
   (a) (5pts) $D_x(\cosh(e^x))$

   (b) (5pts) $D_x(\ln \sqrt{x})$

   (c) (5pts) $D_x(2x^2+x)$

   (d) (5pts) $D_x(\tan^{-1}(\sqrt{x^2-1}))$

   (e) (5pts) $D_x((3x)^{2x})$
2. (5pts) Find a formula for \( f^{-1}(x) \) if 
\[
f(x) = \sqrt[3]{2x + 8}.
\]
**Note:** \( f^{-1}(x) \) is the inverse of \( f(x) \). It is **not** equal to \( \frac{1}{f(x)} \).

3. (10pts) Evaluate the following:

   (a) \( \sin^{-1} \left( \frac{\sqrt{3}}{2} \right) = \) ________________

   (b) \( \tan^{-1}(-1) = \) ________________

   (c) \( \cos^{-1} \left( \cos \left( \frac{\pi}{2} \right) \right) = \) ________________

   (d) \( \sin^{-1} \left( \sin \left( \frac{3\pi}{4} \right) \right) = \) ________________

   (e) \( \sin \left( \cos^{-1} \left( \frac{4}{5} \right) \right) = \) ________________

4. (10pts) There are initially 10 bacteria in a petri dish. After one hour, there are 32 bacteria. Let \( P(t) \) denote the population of the bacteria after \( t \) hours. Note that \( P(0) = 10 \) and \( P(1) = 32 \).

   (a) (6pts) Find a formula for \( P(t) \) assuming the population grows exponentially.

   (b) (4pts) How long will it take before there are 100 bacteria in the petri dish? No need to simplify.
5. (24pts) Evaluate the following indefinite integrals. Remember $+C$!!

(a) $\int \sin(2x) \cos(3x) \, dx$

(b) $\int x \cos(2x) \, dx$

(c) $\int x^2 \ln x \, dx$

(d) $\int \tan^3 x \, dx$
6. (11pts) Evaluate the indefinite integral
\[ \int x\sqrt{4-x^2} \, dx \]
in two different ways:

(a) (3pts) First, using the substitution \( u = 4 - x^2 \).

(b) (8pts) Second, using the rationalizing substitution \( x = 2 \sin t \).

Note: You must show all of your steps to get full credit on this portion.

7. (10pts) Find \[ \int \frac{1}{(x + 3)(x - 4)} \, dx \]
Trigonometric Formulas:

\[
\begin{align*}
\sin^2 x + \cos^2 x &= 1 \\
1 + \tan^2 x &= \sec^2 x \\
\sin^2 x &= \frac{1}{2}(1 - \cos 2x) \\
\cos^2 x &= \frac{1}{2}(1 + \cos 2x) \\
\sin 2x &= 2 \sin x \cos x \\
\sin x \cos y &= \frac{1}{2}\left(\sin(x - y) + \sin(x + y)\right) \\
\sin x \sin y &= \frac{1}{2}\left(\cos(x - y) - \cos(x + y)\right) \\
\cos x \cos y &= \frac{1}{2}\left(\cos(x - y) + \cos(x + y)\right)
\end{align*}
\]

Inverse Trigonometric Formulas:

\[
\begin{align*}
D_x \sin^{-1} x &= \frac{1}{\sqrt{1 - x^2}} \quad -1 < x < 1 \\
D_x \cos^{-1} x &= -\frac{1}{\sqrt{1 - x^2}} \quad -1 < x < 1 \\
D_x \tan^{-1} x &= \frac{1}{1 + x^2} \\
D_x \sec^{-1} x &= \frac{1}{|x|\sqrt{x^2 - 1}} \quad |x| > 1
\end{align*}
\]

Hyperbolic Trigonometric Formulas:

\[
\begin{align*}
\cosh x &= \frac{e^x + e^{-x}}{2} \\
\sinh x &= \frac{e^x - e^{-x}}{2} \\
\tanh x &= \frac{\sinh x}{\cosh x} \\
\cosh^2 x - \sinh^2 x &= 1 \\
D_x \sinh x &= \cosh x \\
D_x \cosh x &= \sinh x
\end{align*}
\]