

Math 1060 ~ Trigonometry

1 Degree and Radian Measures of Angles

Learning Objectives

In this section you will:

- Convert between degree and radian measures.
- Graph angles in standard position.
- Determine coterminal angle measures in degrees and radians.
- Determine supplementary and complementary angles.

$\sin^2 u + \cos^2 u = 1$

$\sin 2u = 2 \sin u \cos u$

$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

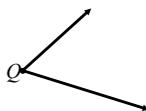
$c^2 = a^2 + b^2 - 2ab \cos C$

Vocabulary for angles

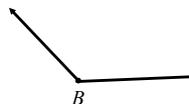
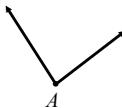
ray



angle



vertex

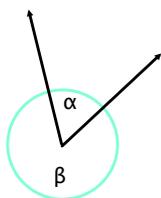


straight angle

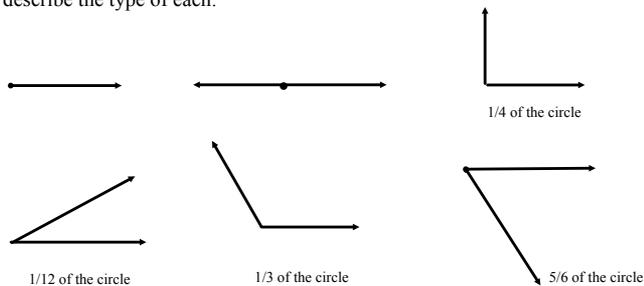


C

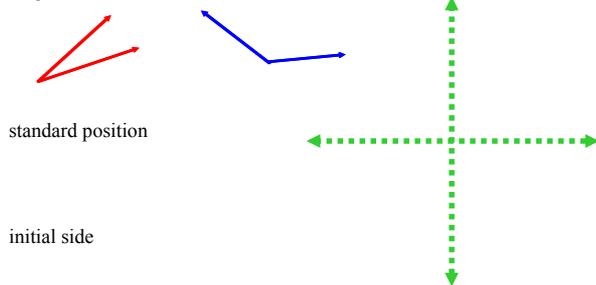
Degree Measure of Angles and Types of Angles



Ex 1: State the measure of each of these angles in degrees and describe the type of each.



Angles in Standard Position



standard position

initial side

terminal side

positive angle

negative angle

coterminal angles

Ex 2: State a coterminal angle between 0° and 360° for each of these.

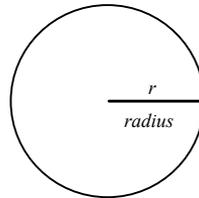
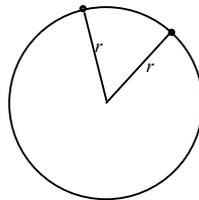
- a) $\alpha = 432^\circ$ b) $\beta = -25^\circ$ c) $\gamma = 500^\circ$ d) $\theta = -630^\circ$

Radian Measure of an Angle

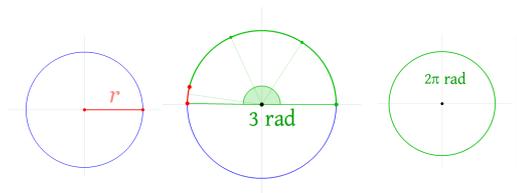
What is the number π ?

A radian is that portion of the circle equal in length to one radius of that circle.

$r =$
 $s =$
 $\theta =$

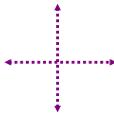


https://en.wikipedia.org/wiki/File:Circle_radians.gif

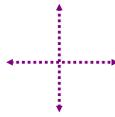


Ex 3: Graph each of these angles in standard position and classify them according to where their terminal side lies. State another coterminal angle between -2π and 2π for each angle.

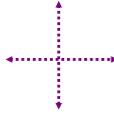
a) $\alpha = \frac{\pi}{3}$



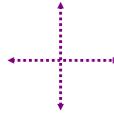
b) $\beta = -\frac{5\pi}{6}$



c) $\lambda = \frac{\pi}{2}$



d) $\theta = \frac{9\pi}{4}$



Converting Between Degrees and Radians

The conversion factor between degrees and radians is

$$2\pi \text{ radians} = 360^\circ.$$

Ex 4: Convert the following measures.

a) 225° to radians

b) $-\frac{5\pi}{6}$ radians to degrees

c) 2 radians to degrees

d) 1080° to radians

Supplementary and Complementary Angles in Degrees



Ex 5: Determine the complement and supplement (if they exist) for each of these angles.

angle	complement	supplement
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a) $\alpha = 24^\circ$

b) $\beta = 90^\circ$

c) $\gamma = 130^\circ$

d) $\varphi = 180^\circ$

Supplementary and Complementary Angles in Radians



Ex 6: Determine the complement and supplement (if they exist) for each of these angles.

angle	complement	supplement
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a) $\alpha = \frac{\pi}{3}$

b) $\beta = \frac{5\pi}{6}$

c) $\gamma = \frac{\pi}{4}$

d) $\varphi = \pi$