

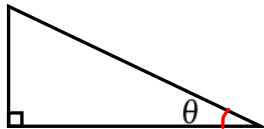
## Trig 1.3 ~ RIGHT TRIANGLE TRIGONOMETRY

In this lesson you will learn to:

- Evaluate trigonometric functions of acute angles in a right triangle.
- Use the fundamental trigonometric identities.
- Use a calculator to evaluate trigonometric functions.
- Use trigonometric functions to model and solve problems.

Right triangle with an acute angle  $\theta$ .

Label the hypotenuse.  
Label the side opposite  $\theta$  .  
Label the side adjacent to  $\theta$  .



$$\sin \theta =$$

$$\cos \theta =$$

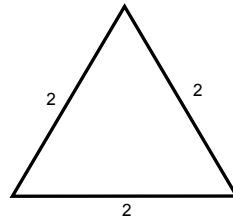
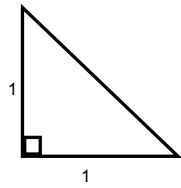
$$\tan \theta =$$

$$\csc \theta =$$

$$\sec \theta =$$

$$\cot \theta =$$

Let's verify with two special triangles:



$$\sin 45^\circ =$$

$$\cos 45^\circ =$$

$$\tan 45^\circ =$$

$$\sin 60^\circ =$$

$$\cos 60^\circ =$$

$$\tan 60^\circ =$$

$$\sin 30^\circ =$$

$$\cos 30^\circ =$$

$$\tan 30^\circ =$$

Notice that co-functions of complementary angles are equal.

$$\sin(90^\circ - \theta) = \cos \theta$$

$$\tan(90^\circ - \theta) =$$

$$\sec(90^\circ - \theta) =$$

Trigonometric identities:

*Reciprocal Identities:*

$$\sin \theta =$$

$$\cos \theta =$$

$$\tan \theta =$$

*Quotient Identities:*

$$\tan \theta =$$

$$\cot \theta =$$

*Pythagorean Identities:*

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

Example 1:

Two ways to get information:

Right triangle

Use identities

If  $\tan \theta = 2$ , find  $\sec \theta$ .

Using a calculator to evaluate trigonometric functions.

Use your calculator (be careful of the mode, radians or degrees) to determine these:

$$\sin 35^\circ$$

$$\cos 75^\circ$$

$$\tan 20^\circ$$

$$\sec 24^\circ$$

$$\cot 15^\circ$$

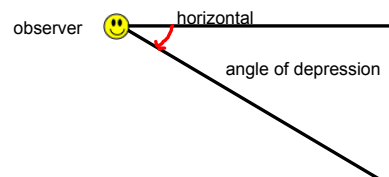
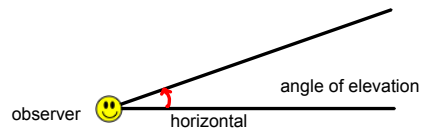
$$\csc 80^\circ$$

$$\tan \pi/8$$

$$\sec 3\pi/5$$

$$\csc 2\pi/5$$

Angles when sighting



Example 2:

Solving problems using right triangles.

- Draw a picture.
- Label known parts.
- Use trigonometric functions to determine desired parts.

If you are standing 50 meters from the base of a tall building and you determine the angle of elevation to the top of the building to be  $80^\circ$ .

a. Determine the height of the building.

b. If you wish to string a wire from you to the top of the building, how long does the wire need to be?