# GRADUATE MATHEMATICS 2007-2008 

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## Preface

This bulletin is prepared annually for graduate students, and those considering graduate study, in the Department of Mathematics. It is intended as a supplement to the bulletin of the University of Utah Graduate School, which is available to all graduate students. The editors of this departmental bulletin welcome suggestions for its improvement from graduate students and members of the faculty.

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## The University of Utah



CALENDAR OF EVENTS FOR 2007-2008

| EVENT | $\begin{aligned} & \text { Fall Semester } \\ & 2007 \end{aligned}$ | Spring Semester $2008$ | $\begin{aligned} & \text { Summer Term } \\ & 2008 \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| Class schedule available on the web | M, Mar 5 | M, Sep 24, 2007 | M, Feb 11 |
| Classes begin | M, Aug 20 | M, Jan 7, 2008 | M, May 12 |
| Last day to drop (delete) classes | W, Aug 29 | W, Jan 16 | W, May 21 |
| Last day to add classes | T, Sep 4 | T, Jan 22 | T, May 27 |
| Last day to elect CR/NC option | T, Sep 4 | T, Jan 22 | T, May 27 |
| Last day to withdraw from term length classes ......... | F, Oct 19 | F, Feb 29 | F, Jun 20 |
| Tuition payment due | T, Sep 4 | T, Jan 22 | T, May 27 |
| Last day to reverse CR/NC option | F, Nov 30 | F, Apr 18 | F, Jul 25 |
| Classes end | F, Dec 7 | W, Apr 23 | W, Jul 30 |
| Reading Day | F, Dec 8 | H, Apr 24 | N/A |
| Final exam period | M-F, Dec 10-14 | F-H, Apr 25-May 1 | H-F Jul 31-Aug 1 |
| Grades available on the web | H, Dec 27 | T, May 13 | T, Aug 12 |
| Annual University Commencement/Convocation Exercises |  | F, May 2 |  |

Departmental Written Qualifying Exams (Prelims) .... M-W, Aug 13-15, 2007 and W-F, Jan 2-4, 2008
Math Dept. TA training for new graduate students Aug. 8-17, 2007

## HOLIDAYS, RECESSES, BREAKS <br> (No classes, day or evening. University closed on holidays)

## Fall Semester 2007

Labor Day Holiday . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . M, Sep 3
Fall Break .................................................................................................... M-F . Oct 8-12
Thanksgiving Break . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . Th-F, Nov 22-23
Holiday Recess ................................................................................... . Sa, Dec 15-Su, Jan 6
Spring Semester 2008
Martin Luther King/Human Rights Day Holiday ...................................................... . . M, Jan 21
Presidents' Day Holiday . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . M, Feb 18
Spring Break
M-Sa Mar 17-22

## Summer Term 2008

Memorial Day Holiday . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . M, May 26
Independence Day Holiday . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . F, Jul 4
Pioneer Day Holiday . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . H, Jul 24
For additional information concerning registration dates and fee payment deadlines see the university schedule(s) at http://www.sa.utah.edu/regist/pages/Deadlines.html. Please note that these dates may change after printing.

## GENERAL INFORMATION

## A Brief History

The University of Utah is a state tax-supported, coeducational institution. Founded in 1850, it is the oldest state university west of the Missouri River. In recent years, the Graduate School has been awarding approximately 215 Ph.D. degrees per year. The University faculty consists of approximately 3100 members.

The Mathematics Department of the University of Utah now awards, on the average, about eight Ph.D. degrees per year. A total of 220 people have earned this degree since 1954. Most of them have positions in state and private universities, but some hold nonacademic positions. Six have been awarded Sloan Research Fellowships, 12 have been visiting members of the Institute for Advanced Study in Princeton, and five have been awarded National Science Foundation Postdoctoral Fellowships.

Our present graduate faculty numbers 45 . A number of the current faculty have received national awards including Sloan Fellowships and Presidential Young Investigator Awards. The University has also recognized members of our faculty with Distinguished Professor, University Distinguished Researcher and Teaching Awards. A list of current members of the faculty, with some of their papers, is included on pp .38 . The research interests of the faculty are the areas of specialization available for graduate studies. They include diverse areas in pure and applied mathematics such as algebraic geometry, arithmetic geometry, commutative algebra, differential geometry, geometric topology, group theory, materials and fluids, mathematical biology, mathematical cardiology, mathematical finance, mathematical physiology, numerical analysis, partial differential equations, probability and statistics, representation theory, and stochastic processes.

During the present year, 24 members of the Mathematics faculty are associated with government-sponsored research contracts.

The University's total enrollment is currently about 29,000. During 2006-2007, there were 45 men and 16 women who were Teaching Fellows and Assistants in mathematics. Our graduate students come from different areas of the United States as well as many foreign countries.

## Research Facilities

The newly-remodeled and expanded Mathematics Branch Library collection in theoretical mathematics consists of 190 journal subscriptions, 15,000 bound journals and 12,000 books. In addition, the Marriott Library collection includes numerous books and journals of interest to mathematics researchers and scholars. There are extensive interactive computing facilities available in the Department.

## Computing Facilities

The Department provides outstanding computing facilities for use by faculty, students and staff. In mid2007, the fully-Internetworked workstation and microcomputer configuration included almost 300 systems in a range of models from these architectures:

- Apple Macintosh (36);
- DEC Alpha (2);
- Intel IA-64 Itanium (1);
- Sun AMD64 Opteron (11);
- Intel IA-32 Pentium and AMD Athlon (14);
- PowerPC GNU/Linux (1)
- Silicon Graphics (3);
- Sun Ray stations (214);
- Sun SPARC (16);

These include at least one file server from each UNIX architecture. Operating systems and CPU types include Solaris (AMD64, SPARC, and IA-32), GNU/Linux (Alpha, AMD64, IA-32, IA-64, MIPS, PowerPC, and SPARC), FreeBSD (IA-32), IRIX (MIPS), MacOS (PowerPC), Minix (IA-32), NetBSD (IA-32), OpenBSD (IA-32), Plan 9 (IA-32), and Windows (IA-32 and AMD64).

A quad-processor 1.05 GHz UltraSPARC-IV Sun Enterprise 2900 file server provides 10TB of storage, with a real-time mirror in another building to supply automatic switch-over should any storage or network component, or electrical power, fail.

Web and FTP services are each provided by separate operating-system domains on the central file server.
WeBWorK course services are handled by two quad-processor Sun W4100 (AMD64 Opteron) servers.
Sun Ray services on the Solaris SPARC architecture are handled by six quad-processor Sun Fire V440 systems, a quad-processor Sun Fire V480 system, and a quad-processor Sun Fire V880 system, and on the GNU/Linux AMD64 architecture by an eight-processor Sun Fire X4600 system.

Batch computing services are provided by a dual-processor Itanium- 2 server, two quad-processor AMD64 servers, and a quad-processor Apple Xeon Xserve system.

All servers are located in a central machine room with its own cooling system and emergency power system, and network hubs share the same reliable power system.

All filesystems are backed up nightly to tapes covering the last few months.
The Mathematics and Physics Department student laboratories are open to members of either department, increasing the access possibilities; computer accounts are, however, managed within each department.

Each user has just one home directory, independent of login architecture, and all users have login access on all of the public workstations. Most standard programs are available on all architectures.

Eight large classrooms provide large-screen projection systems for workstation and videotape output, and there are two portable projection systems for conference-room display.

There are three Xerox 6360 color laser printers, an HP LaserJet 3700 dn color laser printer, and about 50 distributed laser printers, including three high-volume duplex laser printers in the student laboratories. In addition, there are two Xerox WorkCentre Pro 65 black-and-white digital copier/printer/scanner systems ( 65 pages/minute), a Xerox DocuColor 3535 color digital copier/printer/scanner system ( 35 pages/minute), and a Canon imageRunner 8070 copier/printer ( 80 pages/minute).

All computer systems are reachable from anywhere on the global Internet, including home systems with DSL or cable modem Internet connections.

The facility is connected to the campus air-blown fiber-optic network backbone, which can provide several orders of magnitude in expanded network capacity, as the need arises. All network connections provide $10 \mathrm{Mbs}, 100 \mathrm{Mbs}$, and 1 Gbs secure connections, and all offices have at least four ports.

In summer 2004, the new College of Science wireless network was installed, providing seamless encrypted IEEE $802.11 \mathrm{a} / \mathrm{b} / \mathrm{g}$ wireless coverage in, and between, all buildings in the College. Wireless access controls
are based on University of Utah Network IDs (UNIDs), which also provide entry to campus-wide portals and other network services. Short-term wireless guest accounts are available for visitors through the departmental main office in JWB 233.

In summers 2006 and 2007, the departmental Cisco network backbone was upgraded to support connection speeds from 100 Mbs to 1 Gbs .

Research projects can apply for additional computer resources at the Center for High-Performance Computing on a 1024-node AMD64 Opteron cluster installed in mid-2004. Visit the CHPC Web site http: / /www. chpc.utah. edu/ for further details.

For more information about the Department and its activities and facilities, visit its Web site at http: //www.math.utah.edu/.

## Applications

To apply to the Mathematics Department degree program, you must apply to both the Mathematics Department and the University Admissions Office. Application materials and individualized application checklists may be found on our Web site http: / /www. math. utah.edu/grad/. The University application deadlines are November 1st for Spring admission, March 15th for Summer admission, and April 1st for Fall admission. The Mathematics Department deadline for teaching-assistantships applications is March 15th.

To expedite your applications for admission, please follow these procedures:

## 1. University of Utah Admissions Office

(a) Apply online, or download the application at
http://www.sa.utah.edu/admiss/appdownload/ and submit it by postal mail.
(b) Supply these required documents:
i. One copy of transcripts from each college or university you have attended, excluding the University of Utah. Transcripts you have had sent to the University of Utah in the past should be on file if you attended the University. Check with the Admissions Office if you have questions regarding this issue.
ii. For international applicants:

- Official transcripts in their original language accompanied by an English translated version.
- Official TOEFL scores, unless applicant has attended a college or university in the U.S. in the last two years.
- A copy of a national ID card or the photo-ID page of a current passport.
(c) Pay the required application fees.
(d) Track your admission status online regularly to verify that all required documents are received and processed.

Note to international applicants: The I-20 form cannot be processed until all documents and fees are submitted to the Admissions Office and the student has been admitted by the program.
2. Mathematics Department
(a) Download and complete the following forms from http://www.math. utah.edu/grad/:
i. Application for Admission;
ii. Additional Application Form;
iii. Letter of Reference Form (print three copies and follow instructions on the form);
iv. Financial Assistance Application (optional).
(b) Supply these required documents:
i. One copy of transcripts from each college or university you have attended. International applicants must provide official transcripts in their original language accompanied by an English translated version.
ii. For international applicants, a copy of the official TOEFL and TSE scores, unless the student has attended a college or university in the U.S. in the last two years.
iii. We do not require GRE scores. However, we encourage submission of GRE mathematics subject scores.
(c) There are no fees to apply to the Mathematics Department Graduate Program.

Admission to graduate status in either a Master's or Ph.D. program requires that students hold a Bachelor's degree, or its equivalent, with a grade point average of at least 3.0 and that they show promise of success in graduate work.

Students are normally admitted at the beginning of the Fall Semester, and financial aid to new students is only offered at that time. It is desirable that applications for teaching fellowships and teaching assistantships, as well as other financial grants, be submitted as early as possible. Applications received before March 15th will automatically be considered for fellowships for the following Fall Semester.

## Financial Aid

Many of the graduate students in mathematics are supported by teaching assistantships (for students admitted to the Master's degree program) and by teaching fellowships (for students admitted to the Ph.D. degree program). (For convenience in this bulletin, teaching fellowship will usually be used to include both teaching assistantship and teaching fellowship, except where it is necessary to make a distinction between them.) Stipends and duties are discussed on p. 19.

The Mathematics Department currently has two interdisciplinary programs funded by the National Science Foundation, and described as follows.

The IGERT (Interdisciplinary Graduate Education and Research Training) Program is an NSF-sponsored fellowship providing funding to U.S. citizens and permanent residents for the study of Mathematical Biology. IGERT students pursue a program of study to include both mathematics and biology coursework as well as laboratory rotations and journal clubs. Since students in the IGERT program are working towards a Ph.D. in Mathematics, they must therefore, satisfy the departmental disciplinary requirements (described elsewhere in this bulletin), as well as additional requirements for the interdisciplinary component of their training. A summary of the requirements can be found on the IGERT website, http://www.math.utah.edu/ igert/.

The Department of Mathematics successfully competed for a multi-year NSF VIGRE (Vertical Integration of Research and Education) grant and several fellowships are now available through this program to U.S. Citizens and Permanent Residents. Awards are made once per year, and each award is for one semester for current students, and two semesters for incoming students. Those awarded receive stipend, a book allowance, and have no teaching duties for the semester. For more information on VIGRE, please visit http://www. math.utah.edu/vigre/.

## Tuition

Tuition (nine hours) is approximately $\$ 1,900$ per semester for Utah residents and $\$ 6000$ per semester for nonresidents. (Tuition rates may change without notice.) The Graduate Tuition Benefit Program administered by the Graduate School waives tuition fees for Teaching Fellows, Teaching Assistants, and Research Assistants; the policy is described at http://www.utah.edu/graduate_school/tbpguidelines. html. All international students are required to pay $\$ 50.00$ each semester to help cover additional administration costs that occur. Supported students who withdraw after the drop deadline from a course covered by their tuition waiver will be financially responsible for the tuition of that course.

## Health Insurance

The University of Utah sponsors a health insurance plan at excellent rates for students, their spouses and their dependent children under age 26. For details, see http://www.studenthealth.utah.edu/ fees.html.

The Graduate School and the Department provide each funded graduate student with a premium subsidy that covers the full cost of group health insurance offered through GM Southwest; see http:/ / web. ut ah. edu/gradschool/hip.html.

## Housing

The University accepts applications for on-campus residence hall and University student apartment housing. Student residence halls provide a single room and a shared bathroom and kitchen. Visit the Web site http://www.orl.utah.edu/ for current information, or contact Office of Residential Living, 5 Heritage Center, University of Utah, Salt Lake City, Utah 84112-2036, (801) 587-2002. Apartment housing for both married and single undergraduate and graduate students is available on campus. Visit the Web site http://www.apartments.utah.edu/ for current information, or contact University Student Apartments, 1945 Sunnyside Avenue, Salt Lake City, Utah 84108, (801) 581-8667.

Off-campus house and apartment listings can be found in the classified section of The Salt Lake Tribune (http://www.sltrib.com/), the Deseret News (http://www.desnews.com/) and the student newspaper, The Daily Utah Chronicle (http: / /www. dailyutahchronicle.com/).

## PROGRAMS OF STUDY

The Mathematics Department offers programs leading to the degrees of Doctor of Philosophy, Master of Philosophy, Master of Arts, Master of Statistics, Master of Science in Mathematics, Master of Science in Computational Engineering and Science (see p. 11), and a Professional Master of Science and Technology Degree (PMST).

## MASTER OF ARTS AND MASTER OF SCIENCE DEGREES

## A. Graduate School Requirements:

The Master of Arts degree requires standard proficiency in one language - French, German or Russian. The Master of Science degree does not have a language requirement. Otherwise, the degree requirements for the M.S. and M.A. degrees are identical.
A number of forms must be filed, and certain time limitations are to be observed. Some remarks are in order relative to these requirements.

1. A comprehensive oral and/or written qualifying examination in mathematics is given, usually after a student has completed at least a year of graduate study. (See below.) The Master's Project may require a final oral examination. This exam is called the project defense or thesis defense and is separate from the comprehensive examination.
2. Each Master's candidate will be assigned an academic advisor upon entering the program. This advisor has the primary responsibility of guiding and evaluating the candidate's progress through the Master's program. Questions concerning the interpretations of degree requirements should be directed to the candidate's advisor.

## B. Departmental Requirements:

## Requisites for the Master's degree in pure mathematics are:

## Course Requirements

1. Math 5210 (real analysis)
2. Math 5310, 5320 (algebra)
3. One 6000 -level sequence consisting of two one-semester courses
4. Four additional one-semester courses at the 5000- or 6000-level

## Graduation Requirements

1. Pass two of the written qualifying exams OR
2. Take an oral comprehensive examination and complete a Masters Project. The options available for this project are as follows:
a. Master's thesis.
b. A curriculum project.
c. Taking additional courses at the 6000 - or $7000-l e v e l$ (nine credits minimum).
3. The total number of semester hours required for the Master's degree in pure mathematics should fall in the range $30-36$.
As specified by requirements of the Graduate School, a description of a nonthesis option and the basis for its selection shall be included with the student's proposed program. This statement and the proposed program of study must then have the approval of the departmental Director of Graduate Studies and be submitted to the Graduate Dean with the proposed program of study. By arrangement with the Graduate School, those students writing Master's theses may use credit hours in courses, numbered 6000 or above and in the general area of specialization of the thesis, to fulfill the 6-12 hours requirement of 6970 (Thesis Research).

## Requisites for the Master's degree in applied mathematics are:

## Course Requirements

1. Either two 6000 -level sequences, or 5210 and three 6000 -level one-semester courses, two of which must form a year-long sequence.
2. Five additional one-semester courses at the 5000- or 6000-level.

## Graduation Requirements

Same as those for the M.S. in pure mathematics.

## A Comprehensive Examination

Such an examination is required by the Graduate School and is separate from the final oral examination in which a thesis is defended. The student's supervisory committee shall specify whether this examination will be an Oral Comprehensive Examination, or a Written Comprehensive Examination, or both. ${ }^{1}$ The Master's Oral Comprehensive Examination will be conducted by the student's committee and should be held at least one semester prior to the semester in which the student plans to complete the requirements for a Master's degree. The written examination will consist of passing the Written Ph.D. qualifying examinations in two areas.

## Remarks and Suggestions

Courses which are offered regularly at the 5000-level include:

## Pure Mathematics:

Math $5210 \quad$ Real Analysis
Math 5310, 5320 Introduction to Modern Algebra
Math 5410, 5420 Ordinary Differential Equations, Dynamical Systems
Math 5520 Introduction to Algebraic/Geometric Topology

## Applied Mathematics:

| Math 5010 | Introduction to Probability |
| :--- | :--- |
| Math 5040, 5050 | Stochastic Processes and Simulation |
| Math 5080, 5090 | Statistical Inference |
| Math 5110, 5120 | Mathematical Biology |
| Math 5610, 5620 | Introduction to Numerical Analysis |
| Math 5710, 5720 | Introduction to Applied Mathematics |
| Math 5740 | Mathematical Modeling |
| Math 5760, 5765 | Introduction to Mathematical Finance |

Students should also be aware of 5000-level offerings in other departments (e.g., courses in Bi ology, Chemistry, Computer Science, Economics, Physics, etc.) which can be applied to fulfill the course requirements for the Master's program in mathematics. Permission to include such courses must be obtained from the student's committee.
All graduate students who have not had an appropriate course in computer programming are strongly encouraged to consult faculty about appropriate classes in programming early in their program.
Students in the Master's program are expected to complete their Master's degree before entering the Ph.D. program. (Only in exceptional cases will permission be given to enter the Ph.D. program without completing the Master's program.) The normal schedule for Master's students who wish to continue for the $\mathrm{Ph} . \mathrm{D}$. is that they apply to the $\mathrm{Ph} . \mathrm{D}$. program during their final year as a Master's student and that they complete the Master's degree at the end of that year. Those who plan to take the written qualifying exam to complete their graduation requirements to the Masters Degree, may take those exams prior to the beginning of the Fall Semester of their second year. Their admission to the Ph.D. Program is contingent on their successful completion of these exams.

[^0]Financial support for the Master's program will be limited to two years. Teaching loads and stipends are indicated on pp. 19.
Anyone wishing to pursue the study of mathematics toward a Ph.D. degree, but whose preparation does not qualify him/her to enter directly into the Ph.D. degree program, should enter the Master's program with the assurances that:

1. It will not hinder nor significantly delay his/her progress since it is the appropriate "next step" toward his/her goal.
2. Courses for the Master's degree will provide the introductory material and motivate the more abstract and theoretical approach to the same subjects in the Ph.D. program. However, successful completion of the Master's degree does not imply automatic acceptance into the Ph.D. program. Acceptance and financial support for the Ph.D. program is awarded on the basis of a review of the application materials submitted, in a single competition among all applicants, irrespective of whether their previous degrees come from the University of Utah or other institutions.

All candidacy forms for the Master's degree should be submitted to the Graduate Coordinator who will forward them to the Graduate School.

## C. Sequence of Procedures for the Master's Degree

There are time requirements and procedures that must be met in the course of completing a Master's degree. The following schedule is designed to help the candidate meet the necessary deadlines.

## Schedule

## 1. First semester of graduate work:

Discuss your proposed program with the Director of Graduate Studies at the beginning of the semester. By the end of the first year, choose a three-person supervisory committee. It is the responsibility of the student to suggest a committee to the Graduate Advisor, who will be the committee chair.
Meet with your advisor towards the end of the Spring Semester to discuss your progress and any changes in your program. Discuss with him/her your chosen area of study and Master's degree project. It may be desirable for the Director of Graduate Studies to make some changes in the committee membership after you choose your area of study and your Master's degree project.
2. One year before you plan to graduate:

Make the final plan for your course work and have it approved by your entire committee. Subsequent changes in the program are to be approved by your committee and reported to the Graduate School. Talk with members of your committee about plans for your comprehensive examination (to be taken early in the second semester of the second year) including topics that might be included on it; those of you choosing to take written qualifying exams should consult with your advisor on the best strategy for taking the exam. Remember, the oral comprehensive exam must be taken before scheduling a thesis or project defense.
3. One semester prior to graduation:

File the Request for Supervisory Committee and Application for Admission to Candidacy for a Master's Degree forms with the Director of the Graduate School. These cannot be filed until at least one semester of graduate work is completed and must be filed at least one semester before you plan to graduate. (These forms can be picked up from the Graduate Coordinator.)
4. Early in your final semester:

Candidates writing a thesis should schedule the (Defense of Thesis) Final Oral Examination with their supervisory committee. A Handbook for Theses and Dissertations is available in the Graduate School Office for details regarding the preparation and presentation of theses. If you are not otherwise enrolled for at least three credit hours during the semester in which you plan to defend your thesis, you must register for three credit hours of "Faculty Consultation" (mathematics 6980) before taking this final oral examination.

For graduation in a particular semester, one copy of the defended, committee approved manuscript must be submitted to the Thesis Office for "Format Approval" four weeks prior to the last day of the semester. For specific dates, consult A Handbook for Theses and Dissertations.
5. Six weeks prior to graduation:

Have an acceptable draft of the thesis in the hands of your advisor. No time can be set for starting to write a thesis, since conditions vary. Consult with your advisor about the estimated time for writing a thesis.
Several drafts of a manuscript are usually required before a final acceptable copy is reached. Consult with members of your committee regarding the stage at which they wish to see a copy.

## 6. Five weeks prior to graduation:

Deliver a copy of the thesis to each member of your committee at least two weeks prior to the examination date.
Review the Graduate School's Graduate Program Calendar for further information about procedures that should be followed in the final semester before graduation.

## Time Limit

A period of four years is allowed to complete degree requirements for a Master's degree. Extensions beyond this four-year limit must be recommended by the supervisory committee and approved by the Dean of the Graduate School. The same time limit applies to M.S., M.A., M.Phil. degrees. Supported students are entitled to tuition waivers for a total of two years or four semesters for Master's degrees.

## Transfer Credit

At most six hours of transfer credit from another university will be allowed in a 36 -hour graduate program toward a Master's degree.

## D. Recommended schedule of study toward a Master's degree with intent to enter the Ph.D. program.

1. Master's degree students who subsequently plan to apply for admission to the Ph.D. degree program should proceed with the following recommended schedule:

## YEAR ACCOMPLISHMENTS

1 Study three 5000-level or 6000-level courses throughout the year. Where at least two 6000-level courses are studied, take at least two written qualifying examinations in the summer before the second academic year.
2 Study at least three courses at the 6000-level or 7000-level throughout the year. Apply for admission to the Ph.D. degree program no later than February 15. Complete the requirements for a Master's degree. Complete the written qualifying examinations by the summer before the next academic year.

Note: The following is quoted from The University of Utah General Catalog 2008-2009, Graduate Information chapter, p. 39:

Time Limit. All work for the Master's degree must be completed within four consecutive calendar years. On recommendation from the student's supervisory committee, the Dean of the Graduate School can modify or waive this requirement in meritorious cases.

## MASTER OF STATISTICS (MATHEMATICS) PROGRAM

A student is admitted to the program by the University Statistics Committee by making application through the Graduate School. If the University Statistics Committee admits the student, the Mathematics Department will admit him/her to its Master's program. No form needs to be signed by the Mathematics Department for this. Upon completion of the student's program, the University Statistics Committee will notify the Graduate School and the Mathematics Department. The degree, Master of Statistics (Mathematics), will be awarded by the Mathematics Department.

## Prerequisites

1. Either a Bachelor's degree in Mathematics, or the equivalent, e.g., two years of Calculus and two senior level mathematics sequences. ${ }^{2}$
2. Math 3070, 3080, 3090, or equivalent.

## Course requirements

1. Math $5010,5080,5090^{3}$
2. Stat 6070
3. One sequence of Math 6010,6020
4. Electives approved by supervisory committee, 15 credits.
5. Math 6960 (Master's project) 3-6 hours.
6. Written Competency examination in applied statistics.
7. Oral examination on project (Math 6960), this is, a "project defense."

## MASTER OF SCIENCE DEGREE PROGRAM FOR SECONDARY SCHOOL TEACHERS OF SCIENCE OR MATHEMATICS

The College of Science of the University of Utah, including the Departments of Biology, Chemistry, Mathematics and Physics, offers a Master's Degree program for certified secondary school teachers of science and mathematics.

Started in 1972 by Acting Dean Allan Davis, the M.S. Degree Program for Secondary School Teachers of Science or Mathematics aims to help practicing teachers acquire a deeper and broader science background. The final goal is improvement in the quality of science and mathematics teaching in secondary schools.

The masters program works like this:
Once accepted into the program, a graduate committee is appointed for the teacher. This committee works with the teacher to determine goals, and design an individualized program. The committee then supervises performance and progress.

Teachers begin their course work at a level compatible with their current knowledge and background. Teachers may take university courses in the subject they currently teach or may choose to focus on an allied area for certification or further enrichment. For example, a teacher who wants a better understanding of mathematical applications might choose to study highly quantitative courses in other sciences. On the other hand, a biology teacher may choose to concentrate on biology only or strengthen a chemistry background. In addition to regular university courses, those seeking the M.S. Degree for Secondary School Teachers may opt to attend seminar-type courses that teach science curriculum and teaching strategies.

Keeping the demands of a teacher's schedule in mind, enrollees are allowed to take fewer credit hours per semester. To complete the degree, each candidate must perform a Master's project, which may consist of lab work, field work, innovative pedagogy or a scholarly study of an advanced topic. A written report of this activity is required. This report will comprise six of the 30 to 33 semester hours required for degree completion.

Since the objective of the M.S. Degree program for secondary teachers of science or mathematics is to improve the quality of science teaching in schools, the desired applicant is a professional science or mathematics teacher who plans to stay in the field.

Admission requirements include:
Applicant must be accepted by an appropriate committee of the college.
Applicant must have a valid teaching certificate and be teaching science or mathematics in a secondary school.

Applicant does not need an academic or teaching major in the science subject he or she currently teaches to enter the program.

[^1]Applicant must have at least three years teaching experience and be recommended by a professional educator who can judge their performance.

Applicant must satisfy university requirements for graduate school admission.

## MASTER OF PHILOSOPHY DEGREE

The Master of Philosophy (M.Phil.) degree requires the same qualifications for admission and scholarly achievement as the Doctor of Philosophy degree except that it does not require a doctoral dissertation. There is not a separate program for this degree. All supervisory committees, requirements in major and allied fields, and qualifying examinations apply to this degree. The Master of Philosophy degree, like the Doctor of Philosophy degree, is a terminal degree, and a student will not be considered a candidate for both degrees in the same department. The M.Phil. degree of a student desiring to pursue a doctorate in the department in which he/she was awarded the M.Phil. may be rescinded only by formal action of the Graduate Council on written request of the student.

## MASTER OF SCIENCE IN COMPUTATIONAL ENGINEERING AND SCIENCE

The University of Utah Department of Mathematics and the School of Computing have established a joint degree program in Computational Engineering and Science (CES). In 2007-2008, the Mathematics members of the CES Coordinating Committee are Aaron Fogelson and Peter Alfeld. The CES program has a Web site at http://www.ces.utah.edu/.

1. To apply for admission into the CES program, a student must:

- Have a background in the core areas of Computer Science, Mathematics, Physics, Electrical Engineering, Chemistry, Mechanical Engineering, etc.
- Complete an application for the CES program, available at
http://www.ces.utah.edu/admission/ces_admissions.html
- Submit the application to the CES Steering Committee.

2. The requirements for the CES MS Degree are posted at
http://www.ces.utah.edu/ces_ms-curriculum.html
They include tracks with thesis, with courses, and with a project.

## PROFESSIONAL MASTER OF SCIENCE AND TECHNOLOGY

The University of Utah Departments of Mathematics, Chemistry, Geology and Geophysics, and Physics have established a different kind of graduate degree Professional Master of Science and Technology (PMST). The PMST is a professional nonthesis, inter-departmental, and inter-disciplinary degree program that fuses multiple science fields with computational, management, and business skills. In this program, students will learn practical skills that will better prepare them for future employment and career changes. Telephone (801) 585-5630 for more program information.

The PMST program has a Web site at http: / /www.utah.edu/pmst/.

1. To gain admittance into the PMST program, a student must:

- Be a graduating senior who is majoring in science.
- Be a working professional looking to pursue a graduate degree.


## PMST Curriculum

36 credit hours

1. Advanced Quantitative Skills ( 9 credits) data analysis, productive computing, reasoning.
2. Transferable Skills ( 9 credits) communication, project management, budgeting, decision making, negotiation skills, business and environmental law, basic interpretation of federal and state regulatory and policy issues.
3. Internship (3 credits) an internship or cooperative education experience in business, industry, commerce, or government agency.
4. Science Track ( 15 credits) Choose one of three science tracks: Computational Science, Science Instrumentation, or Environmental Science.

## DOCTOR OF PHILOSOPHY DEGREE

## A. Graduate School Requirements:

Please visit the Web site http://web.utah.edu/gradschool/ghrequirements.html\# phd for information on the Ph.D. degree requirements.

## B. Departmental Requirements

1. Supervisory Committee. An academic advisor will be appointed for each prospective student prior to their first semester of graduate study. A Supervisory Committee will be appointed for each graduate student by the end of their first year of study. Any student may, at any time, request a change of advisor and/or committee. This request should be made in writing to the Director of Graduate Studies.
The committee initially appointed for a student shall consist of three people, at least one of whom is in an area of the student's major interest. After the written qualifying examinations are passed, the committee shall be expanded to a committee of five as required by the Graduate School. Since a student's interests may change, the committee can be changed to reflect these interests.
The functions of the student's supervisory committee should be advising and evaluating. Specifically:
a. The student should meet with his/her advisor at the beginning of each academic year to plan that year's work, and at least once a semester to discuss progress. The responsibility for setting these meetings rests with the student.
b. The "Proposed Ph.D. Program", required by the Graduate School, should be worked out by the student and his/her committee at an early stage, with revisions later if the committee considers them desirable.
c. Any special requests regarding financial aid or program of study should be submitted to the student's advisor.

## 2. Course Requirements

a. Course requirements for the Ph.D. degree will consist of at least seven sequences numbered 6000 or above, or their equivalent, approved by the student's supervisory committee. The seven sequences required must include at least 14 credit hours of courses numbered 78007970 (topics courses, seminars, thesis research). The Department has made special arrangements with the Graduate School that credit in any of these courses qualifies as "Thesis Research". The graduate student's supervisory committee, if it deems it appropriate, may require additional courses and/or require specific courses.
b. Exceptions to the above regulations must be approved on an individual basis by the Graduate Committee upon recommendation by the student's supervisory committee.
3. Written Qualifying Examinations
a. Time of the written qualifying examinations.

The written qualifying examinations are given in January and August, usually in the week before the beginning of classes.
b. Written qualifying examination restrictions.

The written part of the Ph.D. qualifying examination in mathematics consists of three tests, in the following eight areas:

- Algebra
- Applied Mathematics
- Differential Equations
- Numerical Analysis
- Probability
- Real and Complex Analysis
- Statistics
- Topology and Geometry

Students should choose their tests in consultation with their advisor(s). One purpose of this consultation is to ensure sufficient breadth in the choice of tests. The student's choice of tests must be approved by the student's supervisory committee.
Registration forms for the examination are available from the Graduate Coordinator. A completed form must be returned to the Graduate Coordinator before the end of the semester preceding the exam.
In order to pass the written qualifying examinations, a student must pass three tests. Students entering with a strong background in undergraduate mathematics may attempt to complete all three qualifying exams in August before the beginning of their second year. Those who need to take 5000 -level classes upon entrance will need an additional year to prepare for some exams, but all students should attempt at least one exam in August before the beginning of their second year, and must attempt three exams by August preceding their third year. Students have a final opportunity to complete the exams in January of their third year (after completing five semesters of course work). Failure to pass at this time will result in termination in the graduate program at the end of the third academic year. A student is permitted to take a maximum of three exams each exam period, and may repeat a failed exam only once, and only at the discretion of the student's supervisory committee.

## c. Syllabus.

The syllabi for the qualifying examination are included in this bulletin. These syllabi are the product of long discussions among the faculty in the various areas, and will not change from year to year, unless approved in advance by the Graduate Committee.
An important point for students to recognize is that the tests will be based on the material in the syllabus, NOT on the material in the preceding year's course on the subject. The student is responsible for preparing to be examined in all of the topics listed on the syllabus, whether or not all of the subjects were covered in a particular course on the subject.

## d. Departmental committee on the examination.

The Department Chairman appoints a member of the faculty to make the arrangements for the written qualifying examinations of each academic year. This person will select two members of the faculty, in each of the various areas of the examination, to participate in the preparation and evaluation of the examinations.

## e. Description of the tests.

The test in each area will be a written test of three hours duration. It is hoped that the inclusion of extra questions will reduce the factor of chance, and the student usually will have the option of omitting some of the questions without penalty. The level of the test should be comparable to that of the first-year graduate course in the field. The faculty members responsible for a given test should check to see that the topics covered on the test are compatible with the syllabus. Copies of past examinations are available from the Graduate Program Coordinator. All examinations are proctored.
f. Grading of the tests.

After all the tests in a given area have been graded, the persons responsible for the test decides what is to be a passing score on the examination; in doing so, it is expected that they confer with and enlist the aid of their colleagues in the area of the examination. Student identities are not revealed to the graders.
g. Announcement of results.

Under normal circumstances the student is informed within one week of the end of the examinations of the passing score on each test and is allowed to examine the tests.
h. Appeals.

Exceptions may be granted to these rules in some cases. Grading of examinations may also be disputed. A student wishing to make an appeal will do so through their supervisory committee or the Director of Graduate Studies. These faculty members will assist the student in taking the necessary actions. A student may also enlist the aid of the Graduate Student Advisory Committee to help in the process. The names of the members of GSAC are listed in this bulletin.

## 4. Oral Qualifying Examination.

A student's supervisory committee shall conduct an oral qualifying examination no later than a date in the second semester (April 15 for Spring Semester and November 30 for Fall Semester) which follows the successful completion of the written examination. Students who fail the oral qualifying examination may be given a second examination at the discretion of the student's supervisory committee. Oral examinations may only be repeated once. Responsibility for scheduling the examination rests jointly with the student and his/her advisor. The oral examination is not a test of specific subject-matter retention; rather it is designed to measure the student's overall mathematics maturity and breadth, and his/her skill at chalkboard exposition and verbal exchange. In general the oral examination is concentrated on the area of specialization of the student and related areas. On the other hand, this oral examination is not a thesis defense.
The candidate initiates scheduling, with his/her supervisory committee approval. This examination should be scheduled as soon as possible after a thesis supervisor has been identified.

## 5. Language Requirements.

The Department of Mathematics does not have language requirements for a Ph.D. degree.
6. Final Oral Examination.

The final oral examination, sometimes called the "Thesis Defense," is distinct from the oral qualifying examination. This examination consists of a public thesis defense. The committee meets after the defense to vote on final approval.
7. Teaching Requirements of Ph.D. Candidate.

The Department requires each graduate student who is studying toward a Ph.D. degree to teach a minimum of two courses, or equivalent tutorials, or laboratory supervisions to be carried out over a minimum of one year and a maximum of six years, whenever appropriate.

## 8. Time Limit.

The time limit for completion of degree requirements for the Ph.D. degree, as set by the Department, is seven years. Normal progress is one or two years to pass the preliminary written qualifying examinations and advance to candidacy, and two or three additional years to complete the thesis work. The Graduate School limits the maximum number of years for which tuition waivers are granted to supported students. Currently, this is five years with a Bachelor's degree, or four years with a Master's degree. Entrants with a Bachelor's degree who have taught in our graduate program for four semesters (two years) can request another year of waiver.

## C. Graduate School Schedule of Procedures for the Ph.D. Degree

The Graduate School has prepared the Graduate PhD Program Calendar for students pursuing a graduate degree, available at the Web site http://web.utah.edu/gradschool/phdcalendar. html. See also http://web.utah.edu/gradschool/thesishandbook.html for A Handbook for Theses and Dissertations.

## D. Recommended Schedule of Study Toward a Ph.D. Degree

The following recommended schedules are considered desirable for Teaching Fellows in the Ph.D. degree program. The numbered years are presumed to begin when the Fall Semester begins and end at the start of the next Fall Semester. Some students, especially those who have previously studied in other Ph.D. programs, should be challenged to try to shorten the schedules outlined here. Except where there are extenuating circumstances, Teaching Fellows who fall more than one year behind these schedules, or who fail to complete the written qualifying examination in two years should not expect their teaching fellowships to continue. The following procedure will be followed with a request for a review for extenuating circumstances:

1. The student submits a written request to his/her committee, with a description of the basis of the request.
2. The student's committee reviews the request and submits a written recommendation to the departmental Graduate Committee.
3. The departmental Graduate Committee makes a final decision regarding the request.

## YEAR ACCOMPLISHMENTS

1 Study three 6000-level courses throughout the year. Complete the written qualifying examinations at the end of the summer of the first year.
Study two or three advanced graduate courses. Attend some seminars. Try to select an area of specialty and a thesis adviser. Complete the oral qualifying examination. Complete the written qualifying examination if a second attempt is necessary.
Continue studying some advanced graduate courses. Participate in seminars. Begin work toward a thesis. Complete the oral qualifying examination if not done previously.
Devote primary attention to developing a thesis. Continue participating in advanced courses and seminars. Find some research topics to pursue beyond a thesis. Complete the requirements for a Ph.D. degree.

CONGRATULATIONS!!!

# INSTRUCTIONS FOR THE PREPARATION AND SUBMISSION OF THESES, DISSERTATIONS AND ABSTRACTS 

When accepted in partial fulfillment of the degree requirements, a Master's thesis or doctoral dissertation becomes the property of the University. However, publication rights are reserved to the author, subject to the provisions of research contracts, patent rights, or other agreements made by the author with the University.

A Handbook for Theses and Dissertations to be followed by the candidate in preparation of the thesis or dissertation is available from the Graduate School or the Thesis Editor. Information is included on bibliographic form and format approval, acceptable style manuals, registrar clearance, submission of the thesis or dissertation, submission of abstracts, and special fees.

It is important that the candidate procure a copy of these instructions before he/she begins the writing of the thesis. The student is invited to consult with the Graduate School Thesis Editor, in 302 Park Building, regarding the thesis or dissertations format. When the completed thesis is submitted a final release for graduation must be obtained from the Thesis Editor.

The use of restricted data for theses and dissertations:

1. Supervisory committees are responsible for approving topics for theses and dissertations and the approval must have the informed consent of the degree candidate to do the research requested.
2. No thesis subject may be approved that will prevent the completed thesis from being made available for public use by the time the degree is granted.
3. The supervisory committee shall schedule a public Final Oral Examination at which time the candidate must defend the thesis satisfactorily before the committee gives final approval of the thesis. This examination must be advertised on the campus one week before the examination data. Anyone may attend the presentation of the thesis.
4. The required number of copies of the completed thesis or dissertation must be submitted for public use to the University of Utah Library by the time the degree is granted.
Exceptions to items 2 and 4 above must be approved by the Graduate Council and can only be made by the Council in those cases where a delay is required to:
5. protect the rights of patent applicants,
6. prevent unjust economic exploitation, or
7. protect the privacy of research subjects.

## Department Preparation of Theses, Dissertations and Abstracts

Student theses, dissertations and abstracts which are used toward degree requirements in the Department of Mathematics will not and cannot be typed, duplicated or printed by the departmental secretarial staff with University equipment. Please do not ask for special consideration. These restrictions apply to undergraduate and graduate student theses, dissertations and abstracts. The policy was set by the University, and is endorsed by the College of Science and the Department of Mathematics. Joint papers with faculty, individual nonthesis publications, mathematical reviews and similar publications will be produced by the Department, within the limitations of its resources.

The student should consult the thesis office program calendar frequently to ensure that they are submitting required forms in a timely manner to meet graduation deadlines. Forms are accepted throughout the semester, however, those students wishing a guaranteed graduation in a specific semester must meet the deadline dates listed on their program calendar. The program calendar can be picked up from the graduate program coordinator's office.

# GUIDELINES FOR THE CONTINUATION OF FINANCIAL SUPPORT 

The Department of Mathematics attempts to continue financial support to graduate Teaching Fellows and Teaching Assistants as warranted by the individual student's progress and budgetary limitations. We try to support the very best graduate students available. A grant of support is made to attract excellent students and to maintain them through their residency for a graduate degree in mathematics.

A general description of departmental policy for the continuation of financial support is given below. This policy covers some specific situations, but the Department reserves the option of flexible interpretation and redefinition of policy.

Continued financial support is recommended for graduate Teaching Fellows and Teaching Assistants who are making satisfactory progress in an approved program of study, and who are performing satisfactorily in their teaching duties. Responsible and capable teaching performance is essential for continuation. Incompetent teachers will not be supported, and cases of conspicuous irresponsibility or neglect will be cause for immediate termination. Besides teaching competence, progress toward a degree is the principal requirement for continued support. Each Teaching Assistant or Teaching Fellow must be enrolled and active as a student, in an approved program of study. Conspicuous neglect of courses, or withdrawal from them, can lead to termination of a teaching assistantship or fellowship. There is a withdrawal penalty if a student's registration fall under the minimum requirement of nine credit hours or a student withdraws late from a course.

All graduate TF's and TA's are eligible for the Graduate Tuition Benefit Program support, which is separately administered by the Graduate School. Students receiving the tuition benefit from the University of Utah Graduate School must be full-time matriculated graduate students in good standing. Full-time status for this purpose is registration of at least nine semester credit hours during the regular academic year. The tuition benefit is valid for a minimum of nine graduate credit hours and a maximum of twelve graduate credit hours for each semester, and there are limits on the number of years of eligibility (see http://www.utah.edu/graduate_school/tbpguidelines.html). Students adding and/or dropping courses after the published university deadline(s) will be responsible for paying any fees and tuition incurred for that semester. If current registration falls below nine semester credit hours at any time during the semester, the student becomes ineligible for the tuition benefit and will be billed for the full tuition for that semester. All international students must pay a fee of $\$ 50.00$ each semester that the tuition waiver does not cover.

The following are guidelines and schedules for decisions regarding renewals of financial support:

## Teaching Assistants in the Master's Degree Program

1. At the beginning of Spring Semester, evaluations are made by the Graduate Committee on the progress of Teaching Assistants in their first year of study toward a Master's degree. Decisions are based on teaching performances and on performance and progress in graduate courses. Notification of renewals or nonrenewals are distributed by April 15.
2. Teaching Assistants are supported for at most two years in the Master's degree program. These appointments automatically terminate, without any special notice, at the end of the second academic year in the Master's degree program. Students who have been Teaching Assistants for less than a year, but cannot finish the degree program by the end of the second academic year, may request an extension of support and a decision whether to grant the request will be made by the Graduate Committee. Teaching Assistants who wish to apply for admission to the Ph.D. degree program should talk with their committees and attempt to follow the first schedule outlined on p. 15. Teaching Assistants who apply for teaching fellowships and admission to the Ph.D. degree will have their applications compared with those of all applicants, both at the University of Utah and at other institutions.

## Teaching Fellows in the Ph.D. Degree Program

1. For Teaching Fellows in their first year in the Ph.D. degree program, evaluations are made by the Graduate Committee at the beginning of Spring Semester. Decisions are based on
teaching performances and progress in graduate courses. Notifications of renewals and nonrenewals are distributed by April 15.
2. For Teaching Fellows beyond their first year in the Ph.D. degree program, evaluations are made by the Graduate Committee at the beginning of Spring Semester. Decisions are based on teaching performances and on progress toward a Ph.D. degree, following the schedule outlined on p. 15. Notifications of renewals and nonrenewals are distributed by April 15. In some cases, renewals may be contingent upon the completion of specific requirements, e.g., a satisfactory performance on the qualifying examination, or the identification and pursuit of a suitable program of study and research.
3. Although the official time limit for a Ph.D degree is seven years (see p. 14, \#8), the Department expects students to finish their Ph.D. requirements in at most five years, six years if there are special circumstances, and seven years only if there exists extraordinary reasons. Support for TAs/TFs then is expected to continue for at most five years (three years if the student enters with a Master's degree), any additional support will be given only if the Graduate Committee determines that there is sufficient grounds for continuation. The Graduate School guarantees tuition waivers to Ph.D. students entering with a Bachelor's degree for five years (three years for those entering with a Master's degree). The Graduate Tuition Benefit Program has been modified to extend the benefit for certain graduate students who serve as Teaching Assistants, and who entered with a Bachelor's degree. Such students who have served a minimum of four semesters as a full-time TA may earn an additional year (two semesters) of tuition waiver. Please check the Graduate School Web site for current information.
4. It is extremely important for graduate students to realize that their degree requirements can be met only if they take the written and oral qualifying examinations in a timely manner as outlined on p. 14.

## Special Remarks to Graduate Students:

1. Take your teaching duties seriously and give attention to your obligations to the Department and to your students.
2. You will probably find that the pursuit of a Ph.D. degree in mathematics is a challenge and that it is not possible to plan and follow a rigid schedule toward the degree. While good performances on the qualifying examinations and in graduate classes are expected of students in the Ph.D. degree program, completion of these formal requirements does not in itself necessarily indicate satisfactory progress toward the Ph.D. Participation in seminars, informal discussions with other students and members of the faculty, and many hours of independent study and thought will be critical toward your development of a research thesis. In reality, your study of mathematics will need to be the dominant feature of your life and as such, no outside employment will be allowed for TAs and TFs.
3. The Department of Mathematics sponsors colloquium lectures that are intended primarily for graduate students and members of the faculty. Many of these lectures are presented by mathematicians who are invited from other institutions, and others are presented by members of the departmental faculty. Such a lecture usually includes some expository remarks in the first part, and then perhaps a more specialized discussion toward the end.
The Department considers attendance at these lectures to be an important part of its program for graduate students. There are opportunities to hear about some important current mathematical developments, to receive suggestions of topics for further study, and to acquire familiarity with various areas of mathematics. There is much for you to gain from the lectures even where you have not had previous contact with the mathematical topics that are discussed.

## STIPENDS AND SALARY INFORMATION FOR 2007-2008

The normal teaching load for Teaching Assistant (M.S., M.A. candidate) and Teaching Fellows (Ph.D. candidate) is the equivalent of one four-hour section per semester. Stipends for lighter loads will be in proportion to the load.

## SALARY SCHEDULE FOR 2007-2008 (ACADEMIC YEAR)

|  | 1st year | 2nd year | 3rd year | 4th year |
| :--- | :--- | :--- | :--- | :--- |
| Master's Program | $\$ 14,500$ | $\$ 14,500$ |  |  |
| Ph.D. Program | $\$ 15,500$ | $\$ 15,500$ | $\$ 16,000$ | $\$ 16,000$ |

In the summer, an additional stipend is often available for teaching a course or lab.
Salary levels for students in the IGERT and VIGRE programs are higher; please visit

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http://www.math.utah.edu/research/mathbio/igert/financial.html
http://www.math.utah.edu/vigre/gradfellowships.html
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for details.
Salary checks are issued twice a month and are available from the front desk in the departmental office. You will receive your first check under your 2007-2008 salary on September 7, 2007. Your last check for the academic year will be received on May 22, 2008. Teaching Fellows who do not teach during the summer term are advised to make appropriate financial arrangements in advance for June, July and August.

University Research Fellowships. Each year the faculty are asked to name outstanding students for the University Research Fellowship. In recent years one or two graduate students in mathematics have received a fellowship each year. The amount of the award is $\$ 10,000$, and there are, of course, no teaching duties for a University Research Fellowship. The Department provides additional support, so that the total salary is equivalent to the salary of Teaching Fellows. The departmental deadline for nomination for the University Research Fellowship is January 25th of the year preceding the award. Only doctoral students may apply for this award and the student must have successfully passed all qualifying examinations.

You should find your combined obligations in teaching and studying to be a full-time undertaking. The Department of Mathematics does not permit Teaching Fellows and Teaching Assistants to assume any additional form of employment.

## SUPERVISORY COMMITTEES

Each graduate student will have an advisor and a supervisory committee. The student's advisor will be initially appointed by the Director of Graduate Studies prior to the student's entrance into the program. The supervisory committee will be formed by the end of the student's first year in the program. Students may request a change of advisor or committee member at any time. This request should be made to the Director of Graduate Studies. Initially, each committee will consist of three members of the faculty; committees for Ph.D. degree candidates will later be expanded to a total of five. After an advisor has been appointed, it is the student's responsibility to seek out his/her advisor to discuss a program of study, and to meet periodically with that advisor at least once each semester.

1. The advisor of the committee is usually in the area indicated by the student as his/her potential major interest area. If the student expresses a personal choice, and if the faculty member suggested is not already overworked with advising, this person will usually be appointed.
2. The other two members of the Ph.D. candidate's committee are appointed, in consultation with the student, after the written part of the qualifying examination is completed.
3. If the student's interests change, the committee makeup will be modified appropriately (by the Director of Graduate Studies after consulting the student and his/her committee).
4. The functions of the advisor and the supervisory committee should be:
a. Advising the student regarding a program of study.
b. Evaluating the student's progress in his/her program of study.
c. Reviewing any requests for changes or waivers in the usual requirements.
5. The student should make contact with his/her advisor every semester to discuss progress and possible changes in the program of study. Advisors are requested by the Director of Graduate Studies to make brief comments on each student's progress each semester.
6. A majority of the student's committee is sufficient to approve (or disapprove) his/her program, or petition for an exemption for some requirement. The student, or a dissenting member, can appeal any decision to the Director of Graduate Studies. Such an appeal will usually be reviewed by the departmental Graduate Committee. Appeals or recommendations which implicitly ask for a deviation from Graduate School policy must be reviewed by the Graduate School.

## THE GRADUATE STUDENT ADVISORY COMMITTEE (GSAC)

The Graduate Student Advisory Committee exists for the following reasons:

1. To advise new and continuing graduate students concerning curricula, requirements for degrees and other aspects of the graduate program.
2. To make recommendations to the Department concerning promotion, tenure and retention of faculty members.
3. To participate in the allocation of ASUU funds supplied to the College of Science Student Council.
4. To make whatever recommendations it feels appropriate concerning the graduate program to the Department of Mathematics.
5. To assist the Department in making its policies and requirements fully understood by the graduate students.

This committee shall consist of a number of members, elected in the spring of each year by the mathematics graduate students. For the school year 2007-2008 the members are:

Mike Purcell, Co-Chair<br>Amber Smith, Co-Chair<br>Blerta Shtylla, RPT<br>Jason Preszler, RPT<br>Lyubima Simeonova, RPT<br>Joro Todorov, RPT<br>Elijah Bogart, RPT<br>Dylan Zwick, Colloquium<br>Jennifer Guajardo, Colloquium<br>Mike Purcell, Colloquium<br>Giao Huynh, Colloquium<br>Lindsay Crowl, Refreshments<br>Brittney Bannish, Refreshments<br>Erica Graham, Refreshments<br>Will Malone, Picnic<br>Anna Moore, Picnic<br>Dylan Zwick, Picnic<br>Darci Taylor, Recruitment<br>Yael Algom-Kfir, Recruitment<br>Jennifer Guajardo, Recruitment<br>Matt Housley, Recruitment<br>Jason Preszler, Webmeister<br>Karin Leiderman, Mathematical Biology<br>Joro Todorov, Algebraic Geometry<br>Erin Chamberlain, Algebra<br>Matt Housley, Topology<br>Karim Khader, Probability and Statistics<br>Mike Purcell, Probability and Statistics<br>Russ Richins, Applied Mathematics

## SYLLABI FOR QUALIFYING EXAMINATIONS

## ALGEBRA

## Topics and References

- GROUPS:

Subgroups, quotient groups, cosets, permutation groups, symmetric and alternating groups, homomorphism and isomorphism theorems, p-groups, Sylow subgroups, Abelian groups, solvable groups. Lagrange's Theorem, Cayley's Theorem, Sylow's Theorems, structure of finitely generated Abelian groups.
References: Cohn, Algebra I, 3.1-3.5, 9.1-9.2, 9.4-9.8. Herstein, Topics in Algebra, Ch. 2. Hungerford, Algebra, 1.1-1.6, 2.1-2.2, 2.4-2.7. Jacobson, Basic Algebra I, 1.1-1.10, 1.12-1.13. Lang, Algebra, 1.1-1.6, 1.9-1.10.

- RINGS:

Ideals, quotient rings, polynomial rings, Euclidean rings, principal ideal domains, unique factorization domains, matrix rings, artinian rings, semisimple rings, finite-dimensional algebras. Jacobson radical, Jacobson Density Theorem, Artin-Wedderburn Theorem.
References: Cohn I, 6.1-6.8, 10.1, 10.5. Cohn II, 4.6, 10.1-10.3. Herstein, Ch. 3. Hungerford, 3.13.3, 3.5-3.6, 9.1-9.5. Jacobson I, 2.1-2.3, 2.5-2.7, 2.9-2.11, 2.14-2.16. Jacobson II, 4.1-4.4. Lang, 2.1-2.2, 2.4, 5.2-5.4, 5.6, 17.1-17.5.

- MODULES:

Submodules, quotient modules, semisimple modules, free modules, projective modules, injective modules, tensor products. Structure of finitely generated modules over principal ideal domains.
References: Cohn I, 10.2-10.6. Cohn II, 3.1-3.2, 4.6, 4.10. Herstein, 4.5. Hungerford, 4.1-4.3, 4.54.6. Jacobson I, 3.1-3.8. Jacobson II, 3.5, 3.7, 3.10-3.11, 3.13. Lang, 3.1-3.5, 3.8, 15.2, 16.1.

- LINEAR ALGEBRA:

Vector spaces, dimension, linear transformations, matrices, characteristic polynomials, trace, determinant, rank, rational canonical form, Jordan canonical form, diagonalization. Cayley-Hamilton Theorem, Gaussian elimination, (symmetric) bilinear forms, orthogonal, unitary, and hermitian forms, tensors and exterior algebras.
References: Cohn I, 4.1-4.7, 7.1-7.3, 11.1-11.5. Herstein, 4.1-4.2, 6.1-6.9.

- FIELDS AND GALOIS THEORY:

Extension fields, degrees, roots, geometric constructions, splitting fields, algebraic closure, algebraic and transcendental extensions, separable extensions, Galois groups, fundamental theorem of Galois theory, solvability by radicals, finite fields, primitive elements.
References: Cohn II, Ch. 5, 6.1, 6.3-6.4. Herstein, Ch. 5, 7.1. Hungerford, 5.1-5.7, 5.9. Jacobson I, 4.1-4.13. Jacobson II, 8.1-8.3, 8.7-8.8, 8.14. Lang, 7.1-7.6, 8.1-8.2, 10.6.

- HOMOLOGICAL ALGEBRA:

Exact sequences, complexes, homology, categories, functors, Ext, Tor.
References: Cohn II, 4.1-4.3, 4.8-4.9. Hungerford, 10.1. Jacobson II, 1.1-1.3, 6.1-6.3, 6.5-6.8. Lang, 4.1-4.2.

## APPLIED MATHEMATICS

## Topics

- FINITE-DIMENSIONAL LINEAR OPERATORS:

Spectral theory, Fredholm alternative, generalized inversion, singular value decomposition, minimax principle.

- INTEGRAL AND DIFFERENTIAL OPERATORS:

Contraction Mapping Theorem, compact operators, Hilbert-Schmidt theory, spectral theory, distributions, Green's functions, resolvent operators, method of images, discrete and integral transforms.

- CALCULUS OF VARIATIONS:

Euler-Lagrange equations, Hamilton's principle, approximation techniques.

- COMPLEX VARIABLE METHODS:

Analytic function theory, integral theorems, conformal mappings, contour integration, special functions, transform pairs, scattering theory.

- ASYMPTOTIC EXPANSIONS:

Laplace's method, Watson's lemma, methods of steepest descent and stationary phase.

## Text

- J. P. Keener, Principles of Applied Mathematics: Transformation and Approximation, Addison Wesley (1988) [ISBN 0-201-15674-1, 978-0-201-15674-4].


## Other Texts

- G. Strang, Linear Algebra and its Applications, Harcourt, Brace, Jovanovich (1988) [ISBN 0-15-551005-3, 978-0-15-551005-0].
- B. Friedman, Principles and Techniques of Applied Mathematics, Wiley (1956).
- I. Stakgold, Boundary Value Problems of Mathematical Physics, Vol. 1, Macmillan (1967-1968).
- G. F. Carrier, M. Krook and C. E. Pearson, Functions of a Complex Variable, Hod Books (1983) [ISBN 0-07-010089-6, 978-0-07-010089-3].
- E. T. Copson, Asymptotic Expansions, Cambridge University Press (1967).
- R. Courant and D. Hilbert, Methods of Mathematical Physics, Interscience Publishers (1953-1962).


## DIFFERENTIAL EQUATIONS

## Topics

- Nonlinear analysis: 1. Contraction mapping principle 2. Implicit function theorem in Banach spacesapplications 3. Theory of Brouwer and Leray-Schauder degree 4. Fixed point theorems.
- Existence-uniqueness theorems for initial value problems: 1. Picard-Lindelöf theorem, Cauchy Peano theorem 2. Dependence upon initial conditions and parameters 3. Differential inequalities 4. Theory of linear systems, variation of constants formula. Floquet theory.
- Stability theory: 1. Stability of perturbed linear systems 2. Lyapunov stability.
- Sturm-Liouville problems and spectral theory.
- Hilbert space theory for linear PDE: 1. Distributions 2. Sobolev spaces, trace, Rellich embedding theorem 3. Lax-Milgram theorem 4. Applications of Lax-Milgram to the study of weak solutions of elliptic PDE's 5. Regularity theory 6. Spectral theorem for elliptic operators.
- Hille-Yosida-Phillips semigroup theory: 1. Strongly continuous semigroups of contractions and their generators 2. Hille-Yosida theorem 3. Phillips theorem 4. Parabolic PDE's 5. Unitary groups and the wave equation.


## Text

- Lawrence C. Evans, Partial Differential Equations, American Mathematical Society, Providence, RI (1998) [ISBN 0-8218-0772-2].
- Robert C. McOwen, Partial Differential Equations: methods and applications, Second Edition ed., Prentice Hall, NJ (2003) [ISBN 0-13-009335-1].
- W. Walter, Ordinary Differential Equations, Springer, New York (1998) [ISBN 978-0-387-98459-9].
- H. Amann, Ordinary Differential Equations: An Introduction to Nonlinear Analysis, de Gruyter, Berlin (1990) [ISBN 978-3110115154].
- K. Schmitt and R. Thompson, Nonlinear Analysis and Differential Equations: An Introduction, University of Utah Lecture Notes (200x).
- R. Showalter, Hilbert Space Methods for Partial Differential Equations, EJDE Monographs, Vol. 1 (1994).


## GEOMETRY AND TOPOLOGY

## Topics

- GENERAL TOPOLOGY:

Metric spaces, paracompact spaces, Urysohn's Metrization Theorem, Tychnoff Theorem, Baire Category Theorem, Tietze's Extension Theorem, function spaces, [Dugundji, Singer-Thorpe]

- HOMOTOPY AND COVERING SPACES:

Fundamental group, covering spaces, universal cover, Van Kampen's Theorem, computations of homotopy groups of $\mathbf{R}^{n}, \mathbf{S}^{n}, \mathbf{C} \mathbf{P}^{n}$, etc., higher homotopy groups, homotopy sequence of a pair, Brouwer's Fixed Point Theorem, exact sequences of pairs and fibrations. [Hatcher]

- SIMPLICIAL AND CELL COMPLEXES:

Simplicial complexes, barycentric subdivision, simplicial approximation, etc. [Hatcher]

- HOMOLOGY THEORIES:

Including simplicial (and/or CW) and singular, axioms of a homology theory, universal coefficient theorem. Cohomology, cup products, Poincaré duality. [Hatcher]

- MANIFOLDS:

Differential manifolds, construction of tangent bundle and cotangent bundle, exterior algebras, differential forms, DeRham cohomology, Froebenius theorem, Lie derivative, deRham theorem. Sard's theorem, transversality, degree theory, Gauss-Bonnet Theorem, vector fields, Poincaré-Hopf index theorem. [Guillemin and Pollack, Spivak]

- LIE GROUPS:

Basic definitions, definition of Lie algebra. [Spivak]

## Texts

- V. Guillemin and A. Pollack, Differential Topology, Prentice-Hall (1974) [ISBN 0-13-212605-2, 978-0-13-212605-2].
- M. D. Spivak, A Comprehensive Introduction to Differential Geometry, Publish or Perish (1979) [ISBN 0-914098-83-7 (hard), 0-914098-79-9 (soft), 978-0-914098-83-6 (hard), 978-0-914098-79-9 (soft)] (leisurely treatment of many topics in differential geometry).
- G. E. Bredon, Topology and Geometry, Graduate Texts in Mathematics 139, Springer (1993) [ISBN 0-387-97926-3 (New York), 3-540-97926-3 (Berlin), 978-0-387-97926-7 (New York), 978-3-540-979265 (Berlin)].
- A. Hatcher, Algebraic Topology, Cambridge University Press (2002) [ISBN 0-521-79160-X (hard), 0-521-79540-0 (soft), 978-0-521-79160-1 (hard), 978-0-521-79540-1 (soft)] http: / /www.math. cornell.edu/~hatcher/.


## Supplementary References

- M. P. do Carmo, Differential Geometry of Curves and Surfaces, Prentice-Hall (1976) [ISBN 0-13-212589-7, 978-0-13-212589-5].
- M. J. Greenberg and J. R. Harper, Algebraic Topology: An Introduction, Addison-Wesley (1981) [ISBN 0-8053-3558-7 (hard), 0-8053-3557-9 (soft), 978-0-8053-3558-3 (hard), 978-0-8053-3557-6 (soft)].
- J. R. Munkres, Topology-A First Course, Prentice-Hall (1975) [ISBN 0-13-925495-1, 978-0-13-925495-6].
- W. S. Massey, A Basic Course in Algebraic Topology, Springer (1991) [ISBN 0-387-97430-X, 978-0-387-97430-9].
- J. J. Rotman, Algebraic Topology, Graduate texts in mathematics 119, Springer (1988) [ISBN 0-387-96678-1, 978-0-387-96678-6].
- I. M. Singer and J. A. Thorpe, Lecture Notes on Elementary Topology and Geometry, Springer (1967) [ISBN 0-387-90202-3, 978-0-387-90202-9].
- J. Dugundji, Topology, Wm. C. Brown (1989) [ISBN 0-697-06889-7, 978-0-697-06889-7].
- F. W. Warner, Foundations of Differentiable Manifolds and Lie Groups, Springer (1983) [ISBN 0-387-90894-3, 978-0-387-90894-6].
- S. Eilenberg and N. E. Steenrod, Foundations of Algebraic Topology, Princeton (1952) (Chapters 9 and 10, Cech homology).
- B. Gray, Homotopy Theory: An Introduction to Algebraic Topology, Academic Press (1975) [ISBN 0-12-296050-5, 978-0-12-296050-5].
- J. G. Hocking and G. S. Young, Topology, Addison-Wesley (1961).
- W. J. Pervin, Foundations of General Topology, Academic Press (1964).
- T. Benny Rushing, Topological Embeddings, Academic Press (1973) [ISBN 0-12-603550-4, 978-0-12-603550-6] (1.3, 1.4, 1.6D, 1.8, 2.2, 3.2).
- E. H. Spanier, Algebraic Topology, Corrected ed., Springer (1981) [ISBN 0-387-90646-0, 978-0-387-90646-1] (Chapter 2: Fibrations).
- N. E. Steenrod, The Topology of Fibre Bundles, Princeton (1951) (Ch. 1: Coordinate bundles and fibre bundles).
- S. Sternberg, Lectures on Differential Geometry, Prentice-Hall (1964).
- J. W. Vick, Homology Theory: An Introduction to Algebraic Topology, Academic Press (1973) [ISBN 0-12-721250-7, 978-0-12-721250-0], J. W. Vick, Homology Theory: An Introduction to Algebraic Topology, 2nd ed., Springer (1994) [ISBN 0-387-94126-6 (New York), 3-540-94126-6 (Berlin), 978-0-387-94126-4 (New York), 978-3-540-94126-2 (Berlin)].


## NUMERICAL ANALYSIS

## Topics

- NUMERICAL LINEAR ALGEBRA:

Direct and iterative methods for solving linear algebraic equations. Error analysis. Methods for finding eigenvalues and eigenvectors. Singular value decomposition. Least squares.

- INTERPOLATION AND APPROXIMATION:

Polynomial, rational, Fourier Series, spline based methods of interpolation and approximation. Quadrature.

- SOLUTION OF NONLINEAR EQUATIONS AND OPTIMIZATION:

Contraction mapping principle, Newton's method, conjugate gradient method, steepest descent method, quasi-Newton methods, linear programming, constrained optimization.

- NUMERICAL SOLUTIONS OF DIFFERENTIAL EQUATIONS:

Runge-Kutta methods, linear multistep methods for initial value problems of ODEs. Shooting, finite differences, finite elements for boundary value problems of ODEs. Finite difference and finite element methods for simple PDEs.

## Texts

- E. W. Cheney, Introduction to Approximation Theory, 2nd ed., McGraw-Hill (1998) [ISBN 0-8218-1374-9, 978-0-8218-1374-4].
- P. J. Davis, Interpolation and Approximation, Dover (1975).
- J. E. Dennis, Jr. and R. B. Schnabel, Numerical Methods for Unconstrained Optimization and Nonlinear Equations, Prentice-Hall (1983) [ISBN 0-13-627216-9, 978-0-13-627216-8].
- R. Fletcher, Practical Methods of Optimization, Wiley (1987) [ISBN 0-471-27711-8 (vol. 1), 0-471-27828-9 (vol. 2), 978-0-471-27711-8 (vol. 1), 978-0-471-27828-3 (vol. 2)].
- G. H. Golub and C. F. van Loan, Matrix Computations, 2nd ed., Johns Hopkins University Press (1989) [ISBN 0-8018-3772-3 (hard), 0-8018-3739-1 (soft), 978-0-8018-3772-2 (hard), 978-0-8018-3739-5 (soft)].
- J. D. Lambert, Computational Methods in Ordinary Differential Equations, Wiley (1973) [ISBN 0-471-51194-3, 978-0-471-51194-6].
- A. R. Mitchell and D. F. Griffiths, The Finite Difference Method in Partial Differential Equations, Wiley (1980) [ISBN 0-471-27641-3, 978-0-471-27641-8].
- G. Strang and G. F. Fix, An Analysis of the Finite Element Method, Prentice-Hall (1973).
- R. Wait and A. R. Mitchell, Finite Element Analysis and Applications, Wiley (1985) [ISBN 0-471-90677-8 (hard), 0-471-90678-6 (soft), 978-0-471-90677-3 (hard), 978-0-471-90678-0 (soft)].


## PROBABILITY

## Topics

- Probability spaces, expectation, independence, Borel-Cantelli lemmas, Strong Law of Large Numbers.
- Weak convergence, characteristic functions, Central Limit Theorem.
- Conditional expectation, martingale convergence theorem, uniform integrability, optional stopping theorem.
- Countable Markov chains, recurrence, transience, stationarity, ergodicity.
- Brownian motion, sample path properties, Donsker's theorem.


## Texts

- P. Billingsley, Probability and Measure, 3rd ed., Wiley (1995) [ISBN 0-471-00710-2, 978-0-471-00710-4].
- R. Durrett, Probability: Theory and Examples, 2nd ed., Duxbury Press (1996) [ISBN 0-534-24318-5, 978-0-534-24318-0].
- B. Fristedt and L. Gray, A Modern Approach to Probability Theory, Birkhäuser (1997) [ISBN 0-8176-3807-5 (Boston), 3-7643-3807-5 (Basel), 978-0-8176-3807-8 (Boston), 978-3-7643-3807-7 (Basel)].


## REAL AND COMPLEX ANALYSIS

## Topics

- MEASURE THEORY:

Measurable spaces, measurable functions and positive measures. Integrable functions, integrals. Integration on locally compact spaces, Riesz representation theorem, regular Borel measures, Lusin's theorem. Integration on product spaces, Fubini's theorem. Complex measures, Radon-Nikodym theorem. Lp - spaces, duality.

- BASIC FUNCTIONAL ANALYSIS:

Hilbert spaces, Banach spaces, Hahn-Banach theorem, Banach-Steinhaus theorem, open mapping theorem.

## - COMPLEX ANALYSIS:

Holomorphic functions, Cauchy-Riemann equations, Cauchy's theorem, Cauchy's integral formula, Power series, Taylor series of holomorphic functions, isolated singularities, Laurent series, Residue theorem, applications to calculation of definite integrals. Rouche's theorem, Conformal mappings, examples, maximum principle, Schwartz lemma, infinite products, Weierstrass factorization theorem. Analytic continuation, monodromy. Elliptic functions, modular functions and Picard's theorem.

## Texts

- W. Rudin, Real and Complex Analysis, 3rd ed., McGraw-Hill (1987) [ISBN 0-07-054234-1, 978-0-07-054234-1].
- P. R. Halmos, Measure Theory, Graduate texts in mathematics 18, Springer (1975) [ISBN 0-387-90088-8, 978-0-387-90088-9].
- L. V. Ahlfors, Complex Analysis, 3rd ed., McGraw-Hill (1979) [ISBN 0-07-000657-1, 978-0-07-000657-7].
- W. Rudin, Real and Complex Analysis, 3rd ed., McGraw-Hill (1987) [ISBN 0-07-054234-1, 978-0-07-054234-1].
- J. Ogden and E. G. Milewski, Schaum's Outline: The Complex Variables Problem Solver, Research \& Education Association (1987) [ISBN 0-87891-604-0, 978-0-87891-604-7].
- T. M. Apostol, Modular Functions and Dirichlet series in Number Theory, 2nd ed., Springer (1990) [ISBN 0-387-97127-0, 978-0-387-97127-8].


## STATISTICS

- Maximum likelihood estimation and the method of moments. Unbiased estimation and the CramerRao lower bound. Sufficiency, confidence intervals, hypothesis testing, likelihood ratio tests. Chisquared tests of simple and composite hypotheses. Nonparametric methods. Linear and multivariate statistics.


## Texts

- L. J. Bain and M. Engelhardt, Introduction to Probability and Mathematical Statistics, 2nd ed., PWSKENT (1992) [ISBN 0-534-92930-3, 978-0-534-92930-5].
- P. J. Bickel and K. A. Doksum, Mathematical Statistics: Basic Ideas and Selected Topics, 2nd ed., Holden Day (Prentice-Hall) [ISBN 0-13-850363-X, 978-0-13-850363-5].


## SYLLABI FOR UPPER DIVISION AND GRADUATE COURSES AND SEMINARS

The editors have attempted to make this listing as complete and accurate as current information will permit. However, additions, changes and deletions may occur because of enrollments, faculty leaves, availability of texts, and so on.

| $\mathbf{5 0 1 0}$ | Introduction to Probability (Fall, Spring, Summer Semester) |
| :--- | :--- |
| Instructors: | R. Brooks, D. Khoshnevisan, and S. Ethier |
| Text: | D. Stirzaker, Elementary Probability, 2nd ed., Cambridge University Press (2003) [ISBN <br>  <br> Meets with: |
| $0-521-53428-3,978-0-521-53428-4]$ |  |
| Prerequisites: | Math 2210 |
| Topics: | This is a one-semester course in probability theory that requires calculus. Topics include <br> combinational analysis, axioms of probability, conditional probability and independence, <br> discrete and continuous random variables, expectation, joint distributions, and the central |
|  | limit theorem. |

$5030 \quad$ Actuarial Mathematics (Spring Semester)
Instructor: S. Ethier

Text: V. I. Rotar, Actuarial Models: The Mathematics of Insurance, Taylor and Francis ed., (2006) [ISBN 1-58488-586-6]

Prerequisites: Math 5010 (grade B- or better required)
Topics: $\quad$ This is a one-semester course in actuarial models that will help to prepare students for the third actuarial exam. Theory of interest, utility theory, individual and collective risk models, ruin models, survival distribution, life insurance models, annuity models, premiums. Additional topics as time permits.

| 5040, 5050 | Stochastic Processes and Simulation I, II (Fall, Spring Semester) |
| :---: | :---: |
| Instructor: | M. Foondun |
| Text: | R. Durrett, Essentials of Stochastic Processes, Springer (2001) [ISBN 0-387-98836-X, 978-0-387-98836-8] |
| Meets with: | 6810, 6815 |
| Prerequisite: | Math 5010 or equivalent |
| Topics: | This is a two-semester course in stochastic processes and computer simulation that does not involve measure theory. The treatment is mostly rigorous, except that certain technical points may be taken for granted and computer simulation is used to enhance understanding. Topics may include Markov chains, Poisson processes, Markov processes, renewal processes, queueing theory, reliability theory, and Brownian motion. Applications will also be discussed. |

5080, $5090 \quad$ Statistical Inference I, II (Fall, Spring Semester)

Instructors: F. Rassoul-Agha and L. Horváth
Text: L. J. Bain and M. Engelhardt, Introduction to Probability and Mathematical Statistics, 2nd ed., Duxbury (2000) [ISBN 0-534-38020-4, 978-0-534-38020-5]
Prerequisite: Math 5010
Topics: Functions of random variables, limiting distributions, statistics and sampling distributions, point estimation, sufficiency and completeness, special distribution theory, normal sampling theory, parametric estimation, confidence regions, hypotheses testing, introduction to linear models.

| 5110, 5120 | Mathematical Biology I, II (Fall, Spring Semester) |
| :--- | :--- |
| Instructors: | J. Keener and P. Bressloff |
| Texts: | Recommended: L. Edelstein-Keshet, Mathematical Models in Biology (SIAM Classics in |
|  | Applied Mathematics 46), SIAM (2005) [ISBN 0-89871-554-7, 978-0-89871-554-5] and |
|  | G. de Vries, T. Hillen, M. Lewis, J. Muller, and B. Schonfisch, A Course in Mathematical |
|  | Biology: Quantitative Modeling with Mathematical and Computational Methods (SIAM |
|  | Mathematical Modeling and Computation 12), SIAM (2006) [ISBN 0-89871-612-8, |
|  | 978-0-89871-612-2] |
| Meets with: | 6830, 6835 |
| Prerequisites: | Math 2280, 3150, or equivalent <br> Topics: |
|  | Introduction to mathematical models which are used in ecology, cell biology, physiology <br> and genetics. Techniques covered include ordinary, delay and partial differential equations, <br> discrete time dynamical systems, and stochastic processes. Emphasis on modeling a bio- |
|  | logical system with appropriate tools, and using geometric and approximation techniques <br> to derive answers to scientific questions. |
|  |  |


| $\mathbf{5 2 1 0}$ | Introduction to Real Analysis (Spring Semester) |
| :--- | :--- |
| Instructor: | K. Bromberg |
| Text: | G. F. Simmons, Introduction to Topology and Modern Analysis, Krieger Publishing <br> Company (2003) [ISBN 1-57524-238-9, 978-1-57524-238-5] |
| Prerequisites: | Math 3210, 3220, or consent of instructor |
| Topics: | Metric spaces, fixed-point theorems and applications, Lebesgue integral, normed linear <br> spaces, approximation, Fourier series. |

5310, $5320 \quad$ Introduction to Modern Algebra I, II (Fall, Spring Semester)
Instructor: T. de Fernex and A. Singh
Text: L. N. Herstein, Abstract Algebra, 3rd ed., Wiley (2001) [ISBN 0-471-36879-2, 978-0-471-36879-3]
Prerequisite: Math 2250 or 2270 , and Math 2900 or 3210
Topics:
(5310) This course begins with a review of the basic properties of sets and integers and continues with an introduction to group theory. It covers the definitions and basic properties of groups, abelian groups, symmetric groups, normal subgroups, and conjugacy. It also includes basic theorems on the structure of groups, Lagrange's theorem, and Sylow's theorem.
(5320) This course is an introduction to the theory of rings and fields. During the first part of the course, we will study general concepts and the relationship between them: ring, field, ideal, maximal and prime ideal, homomorphism, quotient rings, integral domains and unique factorization domains. We then proceed with an indepth study of various polynomials rings, applying as many of the concepts as possible. The course continues with the study of field extensions, and concludes with nonconstructibility proofs from geometry. Time permitting, we will study finite fields and/or the Galois correspondence.

5410, 5420 Introduction to Differential Equations (Fall, Spring Semester)
Instructor: $\quad$ D. Tucker and G. Gustafson
Text: $\quad$ R. Borrelli and C. Coleman, Differential Equations, 2nd ed., Wiley (2004) [ISBN 0-471-43332-2, 978-0-471-43332-3] (Fall, Spring)
Meets with: 6840, 6845
Prerequisites: Math 2220 and 3310; 2250; or instructor's consent.

Topics: (5410) Systems, existence, uniqueness, dependence on parameters, continuation, solution basis for constant coefficients, modeling, nonlinear systems, Laplace transforms
(5420) Series solutions of differential equations, linearization, rest points and stability, asymptotic stability, functions of mathematical physics, partial differential equations of classical physics (heat, wave, Laplace), Sturm-Liouville systems, orthogood expansion theory, applications.

| 5440 | Introduction to Partial Differential Equations (Fall Semester) |
| :---: | :---: |
| Text: | H. F. Weinberger, First Course in Partial Differential Equations, Dover (1995) [ISBN 0-486-68640-X, 978-0-486-68640-0] |
| Instructor: | K. Schmitt |
| Meets with: | 6850 |
| Prerequisites: | Math 2250 or 2270, 2280 |
| Topics: | Classical wave, Laplace, and heat equations; Fourier analysis; Green's functions; Methods of characteristics. |
| 5470 | Applied Dynamical Systems (Fall Semester) |
| Instructor: | A. Borisyuk |
| Text: | S. H. Strogatz, Nonlinear Dynamics and Chaos, Addison-Wesley (1994) [ISBN 0-201-54344-3, 978-0-201-54344-5] |
| Meets with: | 6440 |
| Prerequisites: | Instructor's permission |
| Topics: | Nonlinear dynamical systems. Bifurcations. Chaos, strange attractors, fractals. Models from biological and chemical systems, and mechanical and electrical oscillators. |


| $\mathbf{5 5 2 0}$ | Introduction to Algebraic/Geometric Topology (Spring Semester) |
| :--- | :--- |
| Instructor: | D. Margalit |
| Text: | W. S. Massey, Algebraic Topology: an Introduction, Springer (1991) [ISBN |
|  | 3-540 |

Prerequisites: Math 4510
Topics: Topology of surfaces. Classification of surfaces. Euler characteristic. Homotopy of maps between topological spaces. Fundamental group of a space. Covering spaces. Applications to group theory and knot theory (as time permits). Degree of mappings of surfaces (if time permits).

| $\mathbf{5 6 0 0}$ | Survey of Numerical Analysis (Spring Semester) |
| :--- | :--- |
| Instructor: | S. Isaacson |
| Text: | J. D. Faires and R. L. Burden, Numerical Methods, 8th ed., Thomson/Brooks/Cole (2003) |
| Meets with: | [ISBN 0-534-39200-8, 978-0-534-39200-0] |
| Prerequisites: | Math 2210, Math 2250 or 2280 |
| Topics: | Numerical linear algebra, interpolation, integration, differentiation, approximation (includ- <br> ing discrete and continuous least squares, Fourier analysis, and wavelets), initial and bound- <br> ary value problems of ordinary and partial differential equations. |
|  |  |


| $\mathbf{5 6 1 0 , 5 6 2 0}$ | Introduction to Numerical Analysis I, II (Fall, Spring Semester) |
| :--- | :--- |
| Instructor: | P. Alfeld |
| Text: | R. Burden and J. D. Faires, Numerical Analysis, 8th ed., Brooks Cole (2004) [ISBN |
|  | $0-534-39200-8,978-0-534-39200-0]$ |
| Meets with: | $\mathbf{6 6 1 0 , 6 6 2 0}$ |
| Prerequisites: | Multivariable calculus, linear algebra, programming ability <br> Topics: |
|  | (5610) Numerical linear algebra, polynomial interpolation, numerical differentiation and <br> integration, nonlinear equations, approximation, optimization. |
|  | (5620) Continuation of Math 5610. Numerical solution of initial and boundary value prob- |
|  | lems of ordinary and partial differential equations. |


| $\mathbf{5 7 0 0}$ | Capstone Course in Mathematics (Fall Semester) |
| :--- | :--- |
| Instructor: | K. MacArthur |
| Text: | To be announced |
| Prerequisites: | Completion of two of the following: Math 3100, 3210, 3320, 4030, 4090 <br> Topics: |
|  | This capstone course examines topics in secondary school mathematics from an advanced <br> perspective. Topics are drawn from Abstract Algebra, Geometry, Analysis, and Number <br> Theory, each rooted in the core secondary school curriculum of number and operations, <br> algebra, geometry, and functions. Students learn to formulate and generalize definitions and <br> theorems that help to unite and explain mathematics. They draw connections between ideas <br> taught separately in different courses. Through their work in this course, they improve their <br> ability to promote their pupils' understanding of mathematics and to make better decisions <br> regarding the direction of their lessons and curriculum. |
|  |  |

5710, $5720 \quad$ Introduction to Applied Mathematics I, II (Fall, Spring Semester)
Instructor: D. Dobson
Text: G. Strang, Introduction to Applied Mathematics, Wellesley-Cambridge Press (1986) [ISBN 0-9614088-0-4, 978-0-9614088-0-0]
Prerequisites: Math 2250, 3150, 3160, 5710
Topics: (5710) Symmetric linear systems, positive definite matrices, eigenvalue problems, equilibrium equations for discrete and continuous systems, boundary value problems in ODEs and PDEs, boundary integrals
(5720) Fourier methods, initial value problems in ODEs and PDEs, conservation laws, network flows and combinatorics, optimization.

| $\mathbf{5 7 4 0}$ | Mathematical Modeling (Spring Semester) |
| :--- | :--- |
| Instructor: | E. Cherkaev |
| Text: | To be announced |
| Meets with: | $\mathbf{6 8 7 0}$ |
| Prerequisites: | Math 5600 or CP SC 5220 |
| Topics: | Development of mathematical models for physical, biological, engineering, and industrial <br> phenomena and problems, using mainly ordinary and partial differential equations. In- <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> volvement of analytical and numerical tools suitable for analysis and visualization of the <br> solutions of these problems. |

$5750 \quad$ Topics in Applied Mathematics: Delay Differential Equations (Fall, Spring Semester)

Instructor: $\quad$ D. Goulet and D. Dobson
Text: To be announced
Meets with: $\mathbf{6 8 8 0}$
Prerequisites: Math 5410/5420 or instructor's permission
Topics: A broad range of theory, techniques and applications; existence, uniqueness, stability, oscillatory and periodic solutions, bifurcations, asymptotic methods, numerical methods, and the use of DDE in current research.

| $\mathbf{5 7 6 0 , 5 7 6 5}$ | Introduction to Mathematical Finance I, II (Fall, Spring Semester) |
| :--- | :--- |
| Instructor: | J. Zhu |
| Text: | S. E. Shreve, Stochastic Calculus for Finance I: The Binomial Asset Pricing Model, |
|  | Springer (2004) [ISBN 0-387-24968-0, 978-0-387-24968-1] |
|  | S.E. Shreve, Stochastic Calculus for Finance II: Continuous-Time Models, Springer (2004) |
|  | [ISBN 0-387-40101-6, 978-0-387-40101-0] |
| Prerequisites: | Math 2280 and 5010, 5040 |
| Meets with: | $\mathbf{6 8 9 0}, \mathbf{6 8 9 5}$ |

Topics: (5760) No arbitrage principle, risk-neutral measure and martigale, Black-Scholes-Merton model, stopping times and American options, random walks and exotic options.
(5765) Brownian motion, Ito's calculus, Markov processes and Kolmogorov equations, Girsanov's theorem, derivation of Black-Scholes formula, some other exotic options, bonds and term-structure models, and an introduction to credit models.

| $\mathbf{6 0 1 0}$ | Linear Models (Fall Semester) |
| :--- | :--- |
| Instructor: | L. Horváth |
| Text: | G. Seber and A. Lee, Linear Regression Analysis, Prentice Hall (2002) [ISBN |
|  | $0-13-044941-5,978-0-13-044941-2]$ |
| Prerequisites: | Math 5010, 5080, 5090, 2270 |
| Topics: | Univariable linear models with applications to regression and ANOVA. |


| $\mathbf{6 0 2 0}$ | Multilinear Models (Spring Semester) |
| :--- | :--- |
| Instructor: | L. Horváth |
| Texts: | G. Seber and A. Lee, Linear Regression Analysis, Prentice Hall (2002) [ISBN |
|  | $0-13-044941-5,978-0-13-044941-2]$ |
|  | R. A. Johnson and D. W. Wichern, Applied Multivariate Statistical Analysis, 5th ed., |
|  | Prentice-Hall (2002) [ISBN 0-13-092553-5, 978-0-13-092553-4] |
| Prerequisites: | Math 6010 |
| Topics: | Multivariate linear models with applications to regression and ANOVA. |


| $\mathbf{6 0 4 0}$ | Mathematical Probability (Fall Semester) |
| :--- | :--- |
| Instructor: | S. Ethier |
| Text: | D. Khoshnevisan, Probability, AMS (2007) [ISBN 0-8218-4215-3] |
| Prerequisites: | Math 6210 |
| Topics: | This is a one-semester graduate course on the foundations of modern probability theory. <br>  <br>  <br>  <br>  <br> Topics include the measure-theoretic construction of probability spaces and random vari- <br> ables, classical convergence theorems, martingale theory, and Brownian motion. |
|  | Mor |


| $\mathbf{6 0 7 0}$ | Mathematical Statistics (Spring Semester) |
| :--- | :--- |
| Instructor: | S. Ethier |
| Text: | No Textbook |
| Prerequisites: | Math 2270, 5080, 5090 |
| Topics: | Review of hypothesis testing and point estimation, introduction to simulations, bootstrap <br> methods, and time series analysis. |


| $\mathbf{6 1 3 0 , 6 1 4 0}$ | Introduction to Algebraic Geometry I, II |
| :--- | :--- |
| Instructor: | Y.-P. Lee |
| Text: | P. Griffiths, Principles of Algebraic Geometry, Springer (1994) [ISBN 0-471-05059-8, |

Prerequisite: Math 6310, 6320, 6130

Topics: (6130) Affine and projective varieties, tangent spaces and singularities, curve theory.
(6140) Surfaces, intersection theory, special varieties, introduction to schemes.

| 6150 | Complex Algebraic Curves (or Riemann surfaces) and Complex Algebraic Surfaces. |
| :--- | :--- |
| Instructor: | Y.-P. Lee |
| Texts: | P. Griffiths and J. Harris, Principles of Algebraic Geometry, Wiley (1978) [ISBN |
|  | $0-471-32792-1]$, |
|  | E. Arbarello and others, Geometry of Algebraic Curves, Springer-Verlag (1985) [ISBN |
|  | $0-387-90997-4,978-0-387-90997-4]$ |
|  | W. Barth, C. Peters, and A. van de Ven, Compact Complex Surfaces, 3rd ed., |
|  | Springer-Verlag (1984) [ISBN 0-387-12172-2, 978-0-387-12172-7] |
| Prerequisite: | Math 6220 |
| Topics: | Material will be selected from Riemann surfaces and algebraic curves, Kaehler geometry, |
|  | Stein manifold theory, compact surfaces, etc. |


| 6170 | Riemannian Geometry (Fall Semester) |
| :---: | :---: |
| Instructor: | A. Treibergs |
| Text: | I. Chavel, Riemannian Geometry: A Modern Introduction, 2nd ed., Cambridge University Press (2006) [ISBN 0-521-85368-0, 0-521-61954-8, 978-0-521-61954-7] |
| Prerequisite: | Math 6510 or consent of instructor |
| Topics: | Riemannian Metrics, Connections, Geodesics and their properties; Completeness. HopfRinow Theorem; Hadamard Theorem. Curvature tensor; Sectional curvature; Ricci and scalar curvature. Space Forms. Cartan's Theorem on recovering the metric from curvature; hyperbolic space and its properties. Theorems of Bonnet-Meyers-Synge. Comparison Theorems. Closed Geodesics. Preissman's Theorem. Cut locus. Conjugate locus. Injectivity radius. Isometric Immersions. Second fundamental form. Isoperimetric inequalities. Toponogov Theorem. Alexandrov's Theorem. Soul Theorem. Sphere Theorem. GromovHausdorff convergence. Collapsing. Ricci Flow and Hamilton's Sphere Theorem. |


| $\mathbf{6 2 1 0}$ | Real Analysis (Fall Semester) |
| :--- | :--- |
| Instructor: | A. Bayer |
| Text: | W. Cheney, Analysis for Applied Mathematics, Springer (2005) [ISBN 0-387-95279-9, <br>  <br> Prerequisite: |
| $978-0-387-95279-6]$ |  |
| Math 5210, 4200 |  |
| Topics: | Measures and integrals, $L_{p}$-spaces, Hilbert spaces, Banach spaces, Fourier series. |


| $\mathbf{6 2 2 0}$ | Complex Analysis (Spring Semester) |
| :--- | :--- |
| Instructor: | Staff |
| Text: | W. Cheney, Analysis for Applied Mathematics, Springer (2005) [ISBN 0-387-95279-9] |
| Prerequisite: | Math 4200, 6210 |
| Topics: | Analytic functions, complex integration, conformal mapping, families of analytic func- <br> tions, zeros of analytic functions, analytic continuation. |


| 6310, 6320 | Modern Algebra I, II (Fall, Spring Semester) |
| :--- | :--- |
| Instructor: | A. Singh |
| Texts: | S. Lang, Algebra, Springer (2002) [ISBN 0-387-95385-X, 978-0-387-95385-4] |
| Prerequisite: | Math 5320 or equivalent <br> group actions, Sylow theorems, permutation groups, solvable and nilpotent groups, free <br> Topics: |
|  | groups and presentations. Rings and modules: Euclidean rings, PIDs, modules over a <br> PID, canonical forms, applications to linear algebra. Fields: field extensions, finite fields, <br> cyclotomic fields, Galois theory, transcendence degree. |

6410, $6420 \quad$ Ordinary/Partial Differential Equations (Fall, Spring Semester)
Instructor: P. Bressloff

Text: F. Verhulst, Nonlinear Differential Equations and Dynamical Systems, 2nd ed., Springer (1996) [ISBN 3-540-60934-2, 978-3-540-60934-6] (6410) and notes by K. Schmitt (6420)

Prerequisite: Math 5210 or instructor's consent.
Topics: Existence/uniqueness/continuity theory for ODEs, linear ODEs, stability theory, invariant manifolds, Sturm-Liouville theory, spectral theory, PDEs of classical physics, Hilbert space methods, variational methods, distributions, regularity.

| $\mathbf{6 4 4 0}$ | Advanced Dynamical Systems (Fall Semester) |
| :--- | :--- |
| Instructor: | A. Borisyuk |
| Text: | No Textbook |
| Meets with: | $\mathbf{5 4 7 0}$ |
| Prerequisites: | Consent of instructor <br> Topics: |
| Basic abstract dynamics; stable, unstable, center manifold theory; index theories; KAM <br> theory; chaos; dimensions of attractors; forced oscillations; applications. |  |
|  |  |


| 6510 | Differentiable Manifolds (Fall Semester) |
| :---: | :---: |
| Instructor: | N. Smale |
| Texts: | M. D. Spivak, A Comprehensive Introduction to Differential Geometry, 3rd ed., Publish or Perish (1999) [ISBN 0-914098-70-5 (vol. 1), 0-914098-71-3 (vol. 2), 0-914098-72-1 (vol. 3), 0-914098-73-X (vol. 4), 0-914098-74-8 (vol. 5), 978-0-914098-70-6 (vol. 1), 978-0-914098-71-3 (vol. 2), 978-0-914098-72-0 (vol. 3), 978-0-914098-73-7 (vol. 4), 978-0-914098-74-4 (vol. 5)] and <br> V. Guillemin and A. Pollack, Differential Topology, Prentice Hall (1974) [ISBN 0-13-212605-2, 978-0-13-212605-2] |
| Prerequisite: | Math 4510 and 5520 |
| Topics: | Manifolds, tangent spaces, orientation, Whitney's embedding theorem, transversality, Sard's theorem, partitions of unity, tubular neighborhoods, fiber bundles, degree theory, vector fields, flows, Lie derivatives, Frobenius' integrability theorem, differential forms, DeRham cohomology. |
| 6520 | Introduction to Algebraic Topology (Spring Semester) |
| Instructor: | K. Bromberg |
| Text: | A. Hatcher, Algebraic Topology, Cambridge University Press (2002) [ISBN $0-521-79160-\mathrm{X}$ (hard), 0-521-79540-0 (soft), 978-0-521-79160-1 (hard), 978-0-521-79540-1 (soft)] |
| Prerequisite: | Math 5520, 6510 |
| Topics: | Simplicial and cell complexes, homology and cohomology with coefficients, excision, Mayer-Vietoris sequence, cup and cap products, DeRham theorem, Euler characteristic, Poincaré-Hopf theorem, higher homotopy groups, long exact sequence of a fiber bundle, elementary homotopy theory. |


| $\mathbf{6 6 1 0 , 6 6 2 0}$ | Analysis of Numerical Methods I, II (Fall, Spring Semester) |
| :--- | :--- |
| Instructor: | P. Alfeld |
| Text: | G. H. Golub and C. F. Van Loan, Matrix Computations, 3rd ed., Johns Hopkins University <br> Press (1996) [ISBN 0-8018-5414-8, 978-0-8018-5414-9] |
| Prerequisite: | Math 5600 or 5620 |
| Topics: | Mathematical and computational analysis of numerical methods in linear algebra, opti- <br> mization, and ordinary and partial differential equations. |


| $\mathbf{6 6 3 0}$ | Numerical Solutions of Partial Differential Equations (Spring Semester) |
| :--- | :--- |
| Instructor: | A. Fogelson |
| Text: | K. W. Morton and D. F. Mayers, Numerical Solution of Partial Differential Equations, |

Prerequisite: Math 6610, 6620, Graduate course in PDE's.
Topics: Review of analysis of numerical methods for linear one-dimensional partial differential equations (accuracy and stability). Solution of multi-dimensional linear and nonlinear PDE problems using multigrid approaches. Introduction to methods for nonlinear hyperbolic problems including level set methods.
$6710 \quad$ Applied Linear Operator and Spectral Methods (Fall Semester)

Instructors: G. Milton
Text: J. P. Keener, Principles of Applied Mathematics: Transformation and Approximation, Addison-Wesley (1988) [ISBN 0-201-15674-1, 978-0-201-15674-4]
Prerequisites: Math 5210, 5410 or equivalent
Topics: The theory of linear operators applied to matrix, differential and integral equations, the Fredholm alternative, spectral theory, inverse and pseudo-inverse operators, HilbertSchmidt theory and eigenfunction expansions, wavelets, and Fast Fourier Transforms. Applications to a variety of problems of physics, biology, and engineering. This course along with Math 6720 forms the basis of the Applied Mathematics qualifying examination.

| $\mathbf{6 7 2 0}$ | Applied Complex Variables, Asymptotic Methods (Spring Semester) |
| :--- | :--- |
| Instructors: | J. Keener |
| Text: | J. P. Keener, Principles of Applied Mathematics: Transformation and Approximation, <br> Prerequisites: <br> Topics:Addison-Wesley (1988) [ISBN 0-201-15674-1, 978-0-201-15674-4] <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> The course will develop complex variable techniques used for studying ordinary and partial <br> differential equations coming from physics. The emphasis is on applications rather than <br> pure theory. <br> Complex variable theory; contour integration, conformal methods and applications to solv- <br> ing differential equations, asymptotic methods for evaluating complicated integrals, trans- <br> forms (including Fourier and Laplace transforms) and their application to solving partial <br> differential equations, wavelets. |


| 6750 | Fluid Dynamics |
| :--- | :--- |
| Instructor: | A. Balk |
| Text: | P. K. Kundu, I. M. Cohen, and H. H. Hu, Fluid Mechanics, 3rd ed., Elsevier Academic |

Prerequisites: Undergraduate ODE and PDE, or Consent of Instructor
Topics: Derivation of equations of fluid dynamics, Euler and Navier-Stokes equations, Bernoulli's theorem, Kelvin's circulation theorem, potential flow, airplane lift, boundary layers, waves in fluids, fluid instabilities, turbulence, dynamics of the atmosphere and ocean.

| 6760 | Continuum Mechanics: Solids |
| :--- | :--- |
| Instructor: | A. Cherkaev <br> Text: |
| R. Batra, Elements of Continuum Mechanics, AIAA (2006) [ISBN 1-56347-699-1, <br> 978-1-56347-699-0] |  |
| Prerequisites: | Consent of Instructor |
| Topics: | Linear and nonlinear elasticity theory, transport phenomena, electromagnetic and elastic <br> wave propagation and variational principles. Additional possible topics include piezoelec- <br> tricity, thermoelectricity, viscoelasticity, magnetic materials, the Hall effect, quasiconvexity <br> and phase transitions, shape memory and composite materials. |

6770, $6780 \quad$ Mathematical Biology I, II (Fall, Spring Semester)
Instructor: A. Fogelson and A. Borisyuk
Text: C. Gardiner, Handbook of Stochastic Methods for Physics, Chemistry and the Natural Sciences, 3rd ed., Springer (2005) [ISBN 3-540-20882-8, 978-3-540-20882-2]
Prerequisite: $\quad 5410,5420$, or consent of instructor
Topics:
(6770) This course will provide an introduction to modeling of all physiology, and will cover approximately the first half of the text.
(6780) In this course we will look at models of aspects of the cardiovascular system including blood flow control and characteristics, flow through branching structures, biochemistry and biomechanics of blood clotting, and signal transduction by vascular cells. Analytical and computational approaches to studying the models are discussed and implemented.

| 6790 | Case Studies in Computational Engineering and Science (Spring Semester) |
| :--- | :--- |
| Instructor: | Staff |
| Text: | To be announced |
| Prerequisite: | Math 5740 |
| Topics: | Two to five faculty members from various disciplines will describe in detail a project in <br> which they are engaged that involves all ingredients of computational engineering and sci- <br> ence: a scientific or engineering problem, a mathematical problem leading to mathematical <br> questions, and the solution and interpretation of these questions obtained by the use of <br> modern computing techniques. Participating faculty will vary from year to year. |

Note: All courses in the 6800 series meet with a 5000 -series course, and are for Ph.D. students only. Extra work is required; this should be arranged with the instructor before the end of the second week of classes. See the 5000 -series entries for descriptions.

| $\mathbf{6 8 0 5}$ | Introduction to Probability (Fall, Spring, and Summer Semester) |
| :--- | :--- |
| Meets with: | $\mathbf{5 0 1 0}$ |
| $\mathbf{6 8 1 0 , \mathbf { 6 8 1 5 }}$ | Stochastic Processes and Simulation I, II (Fall, Spring Semester) |
| Meets with: | $\mathbf{5 0 4 0 , 5 0 5 0}$ |
| $\mathbf{6 8 3 0 , 6 8 3 5}$ | Mathematical Biology I, II (Fall, Spring Semester) |
| Meets with: | $\mathbf{5 1 1 0 , 5 1 2 0}$ |
| $\mathbf{6 8 4 0 , \mathbf { 6 8 4 5 }}$ | Introduction to Differential Equations (Fall, Spring Semester) |
| Meets with: | $\mathbf{5 4 1 0 , 5 4 2 0}$ |
| $\mathbf{6 8 5 0}$ | Introduction to Partial Differential Equations (Fall Semester) |
| Meets with: | $\mathbf{5 4 4 0}$ |
| $\mathbf{6 8 5 5}$ | Survey of Numerical Analysis (Spring Semester) |
| Meets with: | $\mathbf{5 6 0 0}$ |
| $\mathbf{6 8 6 0 , 6 8 6 5}$ | Introduction to Numerical Analysis I, II (Fall, Spring Semester) |
| Meets with: | $\mathbf{5 6 1 0 , 5 6 2 0}$ |
| $\mathbf{6 8 7 0}$ | Mathematical Modeling (Spring Semester) |
| Meets with: | $\mathbf{5 7 4 0}$ |
| $\mathbf{6 8 8 0}$ | Topics in Applied Mathematics (Fall, Spring Semester) |
| Meets with: | $\mathbf{5 7 5 0}$ |
| $\mathbf{6 8 9 0}$ | Introduction to Mathematical Finance I (Fall Semester) |
| Meets with: | $\mathbf{5 7 6 0}$ |
| $\mathbf{6 8 9 5}$ | Introduction to Mathematical Finance II (Spring Semester) |
| Meets with: | $\mathbf{5 7 6 5}$ |
| $\mathbf{7 8 0 0}$ | Moduli of Curves |
| Instructor: | Y.-P. Lee |
| Text: | E. Arbarello and others, Geometry of Algebraic Curves, Springer-Verlag (1985) [ISBN |
| Prerequisite: | Consent of Instructor |
| Topics: | $\quad$ Hilbert schemes |

- Nodal curves
- Deformation theory
- Moduli spaces of curves
- Projectivity of moduli spaces
- Line bundles on moduli spaces
- The Teichmüller point of view
- Smooth Galois covers of moduli spaces
- Cycles on the moduli space of stable curves
- Cellular decomposition of moduli spaces (via hyperbolic geometry)
- First consequence of the cellular decompostion
- Intersection theory of tautological classes
- The Hurwitz scheme

| $\mathbf{7 8 0 5}$ | Seminar in Algebraic Geometry |
| :--- | :--- |
| Instructor: | Staff |
| Text: | To be announced |
| Prerequisite: | Consent of Instructor |
| $\mathbf{7 8 3 5}$ | Seminar in Number Theory (Fall Semester) |
| Instructor: | W. Niziol |
| Text: | No Textbook |
| Prerequisite: | Consent of Instructor |
| $\mathbf{7 8 8 0}$ | Topics in Probability |
| Instructor: | F. Rassoul-Agha |
| Text: | No Textbook |
| Prerequisite: | Consent of Instructor |
| Topics: | Various topics in the area of probability, to be offered on the basis of need or interest. May |
|  | be repeated for credit when the topics vary. |
| $\mathbf{7 8 9 0}$ | Topics in Representation Theory |
| Instructor: | D. Miličić <br> Text: |
| No Textbook |  |
| Topics: | Consent of Instructor |
|  | Various topics in representation theory, to be offered on the basis of need or interest. May |
| be repeated for credit when the topics vary. |  |

## FACULTY 2007-2008

More complete bibliographies are available in the departmental office, and on faculty Web pages accessible via http://www.math.utah.edu/people.html\#faculty.

## DISTINGUISHED PROFESSORS

Keener, James P., California Institute of Technology, 1972. Applied Mathematics
Milton, Graeme, Cornell University, 1985. Applied Mathematics

## PROFESSORS

Adler, Frederick R., Cornell University, 1991. Mathematical Ecology
Alfeld, Peter W., University of Dundee, 1977. Approximation Theory
Balk, Alexander M., Moscow Institute of Physics and Technology, 1988. Nonlinear Phenomena
Bertram, Aaron, UCLA, 1989. Algebraic Geometry
Bestvina, Mladen, University of Tennessee, 1984. Topology
Bressloff, Paul C., Kings College, University of London, 1988. Mathematical Biology
Brooks, Robert M., Louisiana State University, 1963. Topological Algebras
Cherkaev, Andrej V. Leningrad Polytechnical Inst., 1979. Optimal Design and Applications
Cherkaev, Elena, Leningrad University, 1988. Applied Mathematics
Dobson, David C. Rice University, 1990. Applied Mathematics
Ethier, Stewart N., University of Wisconsin, 1975. Applied Probability
Fogelson, Aaron L., New York University, 1982. Computational Fluids, Mathematical Physiology
Folias, Efthymios S., California Institute of Technology, 1963. Applied Mathematics
Golden, Kenneth, New York University, 1984. Applied Mathematics
Gustafson, Grant G., Arizona State University, 1968. Ordinary Differential Equations
Hecht, Henryk, Columbia University, 1974. Lie Groups
Horváth, Lajos, Szeged University, 1982. Probability, Statistics
Khare, Chandrashekhar, Caltech, 1995. Algebraic Number Theory
Khoshnevisan, Davar, University of California, Berkeley, 1989. Probability Theory and Mathematical Statistics

Korevaar, Nicholas J., Stanford University, 1981. Differential Geometry and Partial Differential Equations
Miličić, Dragan, University of Zagreb, 1973. Lie Groups
Roberts, Paul C., McGill University, 1974. Commutative Algebra, Algebraic Geometry
Savin, Gordan, Harvard, 1988. Automorphic Forms
Schmitt, Klaus, University of Nebraska, 1967. Nonlinear Analysis, Differential Equations
Smale, Nathan, University of California, Berkeley, 1987. Differential Geometry
Taylor, Joseph L., Louisiana State University, 1964. Group Representations
Toledo, Domingo, Cornell University, 1972. Algebraic Geometry, Differential Geometry
Treibergs, Andrejs E., Stanford, 1980. Differential Geometry
Trombi, Peter C., University of Illinois, 1970. Lie Groups
Tucker, Don H., University of Texas, 1958. Differential Equations, Functional Analysis

## ASSOCIATE PROFESSORS

Bromberg, Kenneth W., University of California at Berkeley, 1998. Topology
Hacon, Christopher D., UCLA, 1998. Algebraic Geometry

Lee, Yuan-Pin, University of California, Berkeley, 1999. Algebraic Geometry, Symplectic Topology, Mathematical Physics.
Niziol, Wiesława, Princeton University, 1991. Arithmetic Geometry
Singh, Anurag, Univ. of Michigan, 1998. Commutative Algebra
Trapa, Peter, Massachusetts Institute of Technology, 1998. Representation Theory
Zhu, Jingyi, New York University, 1989. Mathematical Finance, Applied Mathematics

## ASSISTANT PROFESSORS

Borisyuk, Alla, New York University, 2002. Mathematical Biology, Applied Mathematics.
Ciubotaru, Dan, Cornell University, 2003. Topological and Lie Groups.
de Fernex, Tommaso, University of Illinois at Chicago, 2002. Algebraic Geometry.
Rassoul-Agha, Firas, New York University, 2003. Probability Theory.
Tanner, Jared, University of California at Los Angeles, 2002. Numerical Analysis.
Wortman, Kevin, University of Chicago, 2003. Geometric Group Theory.

## ADJUNCT ASSOCIATE PROFESSOR

Eyre, David, University of Utah, 1992. Applied Mathematics

## ASSISTANT PROFESSOR (LECTURER)

Bayer, Arend, Bonn University, 2006. Algebraic Geometry
Blanchard, Jeffrey D., Washington University at St. Louis, 2007. Fourier Analysis
Cashen, Christopher, University of Illinois at Chicago, 2007. Group Theory
Dao, Hailong, University of Michigan, 2006. Commutative Rings and Algebras
Du, Jian, Stony Brook University, 2007. Numerical Analysis
Earnshaw, Berton, University of Utah, 2007. Mathematical Biology
Easton, Robert W., Stanford University, 2007. Algebraic Geometry
George, David, University of Washington, 2006. Numerical Analysis
Foondun, Mohammud, University of Connecticut, 2006. Probability Theory
Goulet, David M., California Institute of Techology, 2006. Ordinary Differential Equations
Guevara Vasquez, Fernando, Rice University, 2006. Partial Differential Equations
Hormann, Siegfried, Graz University of Technology, 2006. Statistics
Isaacson, Samuel A., Courant Institute of Mathematical Sciences, 2005. Biology
Jiang, Yunfeng, University of British Columbia, 2007. Algebraic Geometry
Kim, MunJu, Brown, 2004. Mathematical Biology
Kim, Peter, Stanford University, 2007. Mathematical Biology
Klosin, Krzysztof, University of Michigan, 2006. Number Theory
Margalit, Dan, University of Chicago, 2003. Topology
Onofrei, Daniel T., Worcester Polytechnic Institute, 2007. Partial Differential Equations
Paupert, Julien H., University of Pierre-et-Marie-Curie (Paris), 2005. Geometry
Roper, Peter, Loughborough University, 2006. Mathematical Biology
Toth, Damon, University of Washington, 2006. Biology
van Opstall, Michael, University of Washington, 2004. Algebraic Geometry

## ASSOCIATE INSTRUCTORS

Alibegovic, Emina, University of Utah, 2003. Geometry and Topology

Allison, Dennis, University of Houston, 1970 (M.S.). Mathematics Education
Jovanovic-Hacon, Aleksandra, University of California, Los Angeles, 1997 (M.A.). Applied Mathematics
Keir, Marilyn, Stanford University, 1968 (M.A.). Mathematics Education
MacArthur, Kelly, University of Utah, 1995 (M.S.). Mathematics Education

## RESEARCH PROFESSORS

Beebe, Nelson H. F., University of Florida (Gainesville), 1972. Quantum Chemistry
Horn, Roger, Stanford University, 1967. Matrix Analysis

## RESEARCH ASSOCIATE PROFESSOR

Palais, Robert, University of California, Berkeley, 1986. Applied Mathematics
PROFESSORS EMERITI
Carlson, James A., Princeton University, 1971. Algebraic Geometry
Coles, William J., Duke University, 1954. Ordinary Differential Equations
Fife, Paul C., New York University, 1959. Applied Mathematics, Partial Differential Equations
Gersten, Stephen M., Cambridge University, 1965. Group Theory
Glaser, L. C., University of Wisconsin, Madison, 1964. Geometric Topology
Gross, Fletcher I., California Institute of Technology, 1964. Group Theory
Mason, J. David, University of California, Riverside, 1968. Probability
Roberts, Anne D., McGill University, 1972. Analysis
Rossi, Hugo, Massachusetts Institute of Technology, 1960. Complex Analysis
Wolfe, J. H., Harvard, 1948. Geometric Integration Theory


[^0]:    ${ }^{1}$ Both may be required by the committee. A marginal pass of the written examination is one justification for requiring both exams.

[^1]:    ${ }^{2}$ A "sequence" refers to a course that continues through an academic year.
    ${ }^{3}$ If Math 5010, 5080, 5090 was taken while the student was an undergraduate, then either one of Math 6010, 6020, 6040, 6070, or a mathematics sequence listed below is required.

