## Week 3 Examples

**Example 1**: Solve: (1) y'' = -9.8, (2) y'' = -0.04y' - 9.8, both with y(0) = 0, y'(0) = 49.

**Answers**: (1)  $y = -9.8t^2/2 + 49t$ ; (2)  $y = 7350 - 245t - 7350e^{-t/25}$ .

**Example 2**: Let  $w = v\sqrt{\rho/g}$  and  $p = \frac{1}{\sqrt{g\rho}}$  to replace Newton's quadratic drag model  $v' = -g - \rho v|v|$  by pw' = -1 - w|w|. Explain rise model  $pw' = -1 - w^2$  and fall model  $pw' = -1 + w^2$ .

**Example 3**: Solve  $pw' = -w^2 + 1$  and  $pw' = w^2 + 1$  as separable equations. See the previous example. **Answers**:  $w(t) = \tanh(c_1 + t/p)$  and  $w(t) = \tan(c_2 + t/p)$ 

**Example 4:** Verify rise time 4.6 and fall time 4.8 for Newton's quadratic drag model v' = -9.8 - 0.0011v|v|, v(0) = 49. Use textbook formulas or the previous two examples.

**Example 5**: Find the point  $r=r^*$  of zero acceleration in the Jules Verne equation  $r''=-\frac{Gm_1}{(R_1+r)^2}+\frac{Gm_2}{(R_3-r)^2}$ . The answer has symbols. Then calculate  $r^*\approx 339,620,820$  meters for the earth-moon problem. Reference:

http://www.math.utah.edu/~gustafso/s2018/2280/lectureslides/julesVerneDE2008.pdf