## The No Slution Case

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## No Solution Case

A signal equation is a nonzero equation having no variables. It is typically encountered in frame sequences as the equation $0=1$.
When a signal equation occurs in a frame sequence, then we report no solution, because a signal equation is a false equation, implying that the system of equations cannot have a solution.
An Example

$$
\begin{array}{rr}
x+2 y+3 z & =4 \\
-y-3 z & =-1 \\
0 & =1
\end{array} \quad \quad \text { Signal Equation } 0=1
$$

## An Illustration of the No Solution Case

$\qquad$

| $\begin{array}{r} y+3 z=2 \\ x+y=3 \\ x+2 y+3 z=4 \end{array}$ | Frame 1. Original system |
| :---: | :---: |
| $\begin{aligned} x+2 y+3 z & =4 \\ x+y & =3 \\ y+3 z & =2 \end{aligned}$ | Frame 2. <br> swap (1,3) |
| $\begin{aligned} x+2 y+3 z & =4 \\ -y-3 z & =-1 \\ y+3 z & =2 \end{aligned}$ | Frame 3. <br> combo (1, 2,-1) |
| $\begin{aligned} x+2 y+3 z & =4 \\ -y-3 z & =-1 \\ 0 & =1 \end{aligned}$ | Frame 4. Signal Equation $0=1$. combo ( $2,3,1$ ) |

The signal equation $\mathbf{0}=\mathbf{1}$ is a false equation, therefore the last frame has no solution. Because the toolkit neither creates nor destroys solutions, then the first frame, which is the original system, has no solution.

## Perplexing Frames

Values cannot be assigned to any variables in the case of no solution. This can be perplexing, especially in a final frame like

$$
\begin{aligned}
& x=4 \\
& z=-1 \\
& 0=1
\end{aligned}
$$

While it is true that $\boldsymbol{x}$ and $\boldsymbol{z}$ were assigned values, the final signal equation $\mathbf{0}=\mathbf{1}$ is false, meaning any answer is impossible.

There is no possibility to write equations for all variables. There is no solution. It is a tragic error to claim $x=4, z=-1$ is a solution.

