Applied Differential Equations 2250-1 and 2250-2 Midterm Exam 1, Fall 2003

Take-Home Exam Date: Wednesday, 17 September, 2003 Inclass Exam Date: Friday, 19 September, 2003

Instructions. The four problems below are take-home, due on the date above at class time. Answer checks are expected. If maple assist is used, then please attach the maple output.

The remaining 20% of the exam is in class, the last 15 minutes of the hour, one problem, of a type similar to one of the problems below. Calculators, hand-written or computergenerated notes are allowed, including xerox copies of tables or classroom xerox notes. Books are not allowed.

- 1. (Quadrature Equations) Solve by the method of quadrature the initial value problem $y''' = x^3 - xe^{-4x} - \cos 2x$, y(0) = y'(0) = 0, y''(0) = 1. Show all integration steps, by hand. An answer check is required.
- 2. (Separable Equations) Solve the separable problem for equilibrium and non-equilibrium solutions. Identify the *implicit* solution. Find, if possible, an *explicit* solution. Check all answers.

$$10y' = \sin x + \tan x - 25y^2(1 + \sec x)\sin x.$$

- 3. (Linear Equations) Solve the linear equation $2xy'(x) + 7y(x) = \sqrt{x}e^{-2x}$, y(1) = 4. Expected details include the factorization method and all integration steps, by hand. An answer check is required.
- 4. (Application: Torricelli's law) A water tank has the shape of $y = x^{8/7}$ revolved around the y-axis. The depth of the water is 19 feet. After 1 hour and 5 minutes, the drain hole at (0,0) empties the tank to a depth of 9 feet. Find the additional time it takes to empty the tank. Ref: Exercise 1.4-52 and equation 1.4-(24). A same answer is less than 60 minutes.

Please attach this exam or a copy to the front of your submitted exam on the due date. Kindly staple the left upper corner and write your name on all pages. Circle 2250-1 (7:30) or 2250-2 (10:45) at the top of the exam.

Name