MATH 5610 HOMEWORK #7, DUE TUE DEC 6

- 1. K&C 4.1.20 Give an example of a matrix with all positive entries such that $x^T A x$ is sometimes negative. (a 2 × 2 matrix suffices)
- 2. Calculate by hand the Cholesky factorization of

$$\begin{bmatrix} 4 & 4 & -2 \\ 4 & 13 & 1 \\ -2 & 1 & 18 \end{bmatrix}$$

3. Implement the LU algorithm with partial pivoting. (see notes math5610_013.pdf:p162). Please select at step k the largest pivot in a column, i.e. at step k select the pivot i s.t.

$$|u_{ik}| \ge |u_{jk}|$$
 for $k \le j \le n$.

In Matlab this can be easily written as:

 $\begin{array}{ll} \% \ choose \ pivot \ i \\ [\,val\,,i\,] \ = \ {\bf max}(\,{\bf abs}\,(U(\,k\,{:}\,n\,,k\,)\,)\,)\,; \\ i \ = \ i {+}k{-}1; \end{array}$

Please see the class website for sample test code and output, which you are welcome to reuse. Test your algorithm with the following matrices (B&F 6.5.4 a,c)

$$A = \begin{bmatrix} 0 & 2 & -1 \\ 1 & -1 & 2 \\ 1 & -1 & 4 \end{bmatrix} \text{ and } A = \begin{bmatrix} 1 & 1 & -1 & 2 \\ -1 & -1 & 1 & 5 \\ 2 & 2 & 3 & 7 \\ 2 & 3 & 4 & 5 \end{bmatrix}.$$